



# Perception in tone-mapping

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# Cornell Box: a rendering or photograph?

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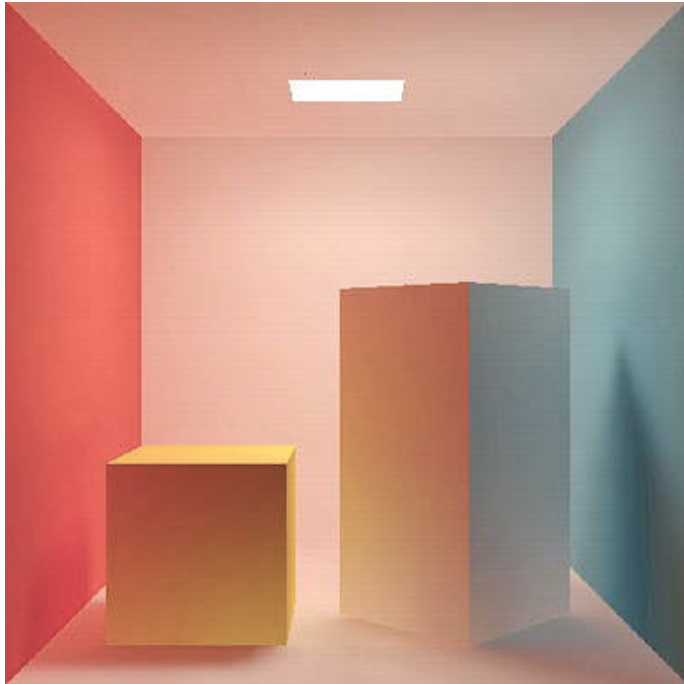
Rendering



Photograph

# Real-world scenes are more challenging

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- ▶ The match could not be achieved if the light source in the top of the box was visible
- ▶ The display could not reproduce the right level of brightness

# Outline

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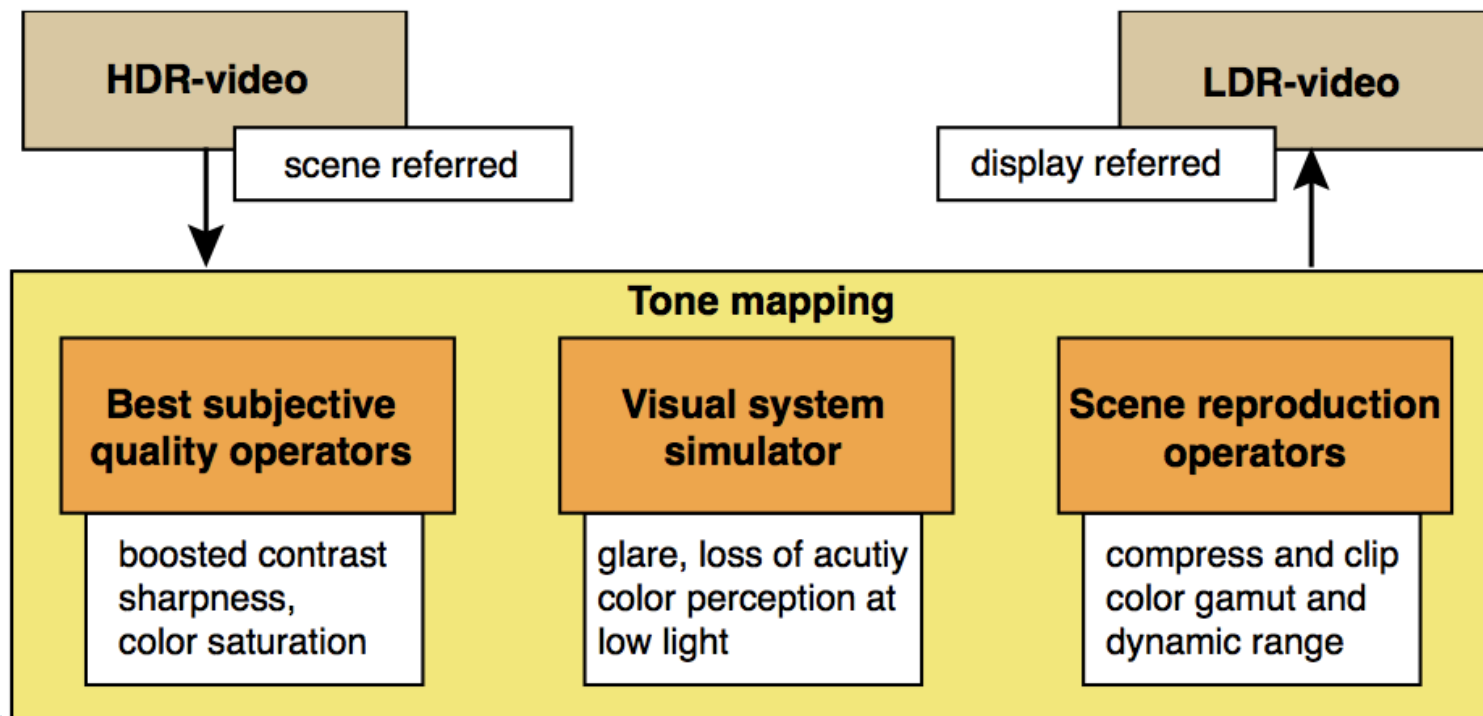
- ▶ **Fundamentals**
  - ▶ Intents of tone-mapping
  - ▶ Display model, luminance and luma
  - ▶ Four approaches to tone-mapping
- ▶ **Perceptual issues**
  - ▶ Color
  - ▶ Glare
  - ▶ Visual metrics-driven TMO
  - ▶ Light and dark adaptation



# Intents of tone mapping

# Three intents of tone-mapping

1. Best subjective quality
2. Visual system simulator
3. Scene reproduction operator



# Intent #1: Best subjective quality

- ▶ Tools
  - ▶ Photoshop
  - ▶ Lightroom
  - ▶ Photomatix
- ▶ Techniques
  - ▶ Color-grading
- ▶ Often artistic intent



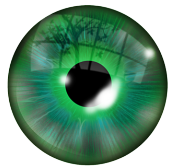


# Intent #2: Visual system simulator

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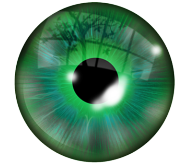


Real-world



The eye adapted to the real-world viewing conditions

The eye adapted to the display viewing conditions



Display

Goal: match color appearance

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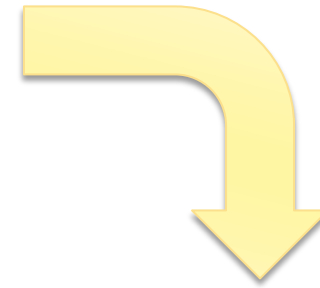


# Intent #3: Scene reproduction problem

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Real-world



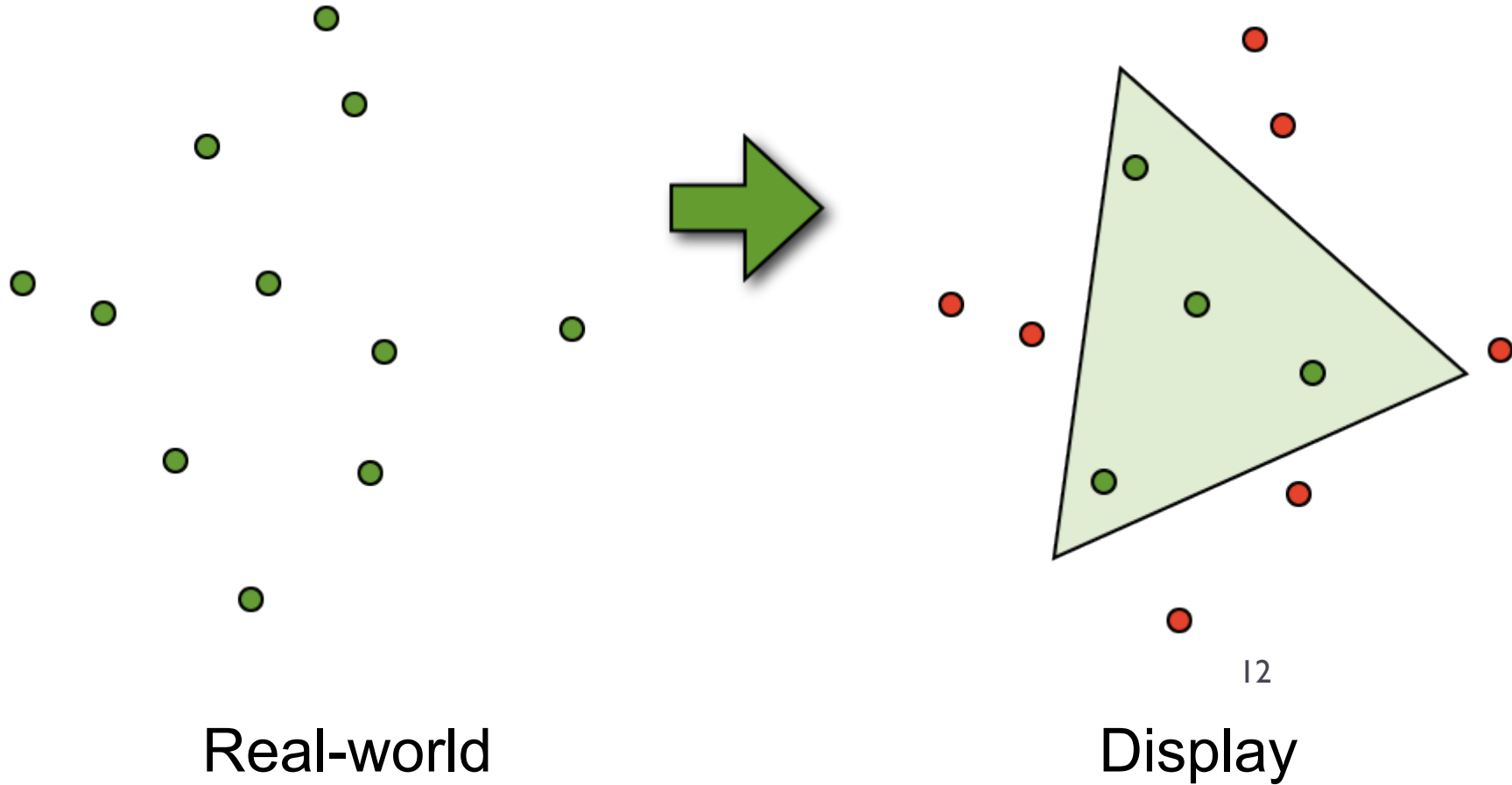
Display

Goal: map colors to a restricted color space



# Mapping problem

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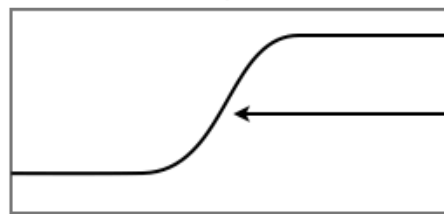


# Display adaptive tone-mapping

Goal: Minimize the visual difference between the input and displayed images



input scene



tone-mapping



display

argmin E

Visual metric

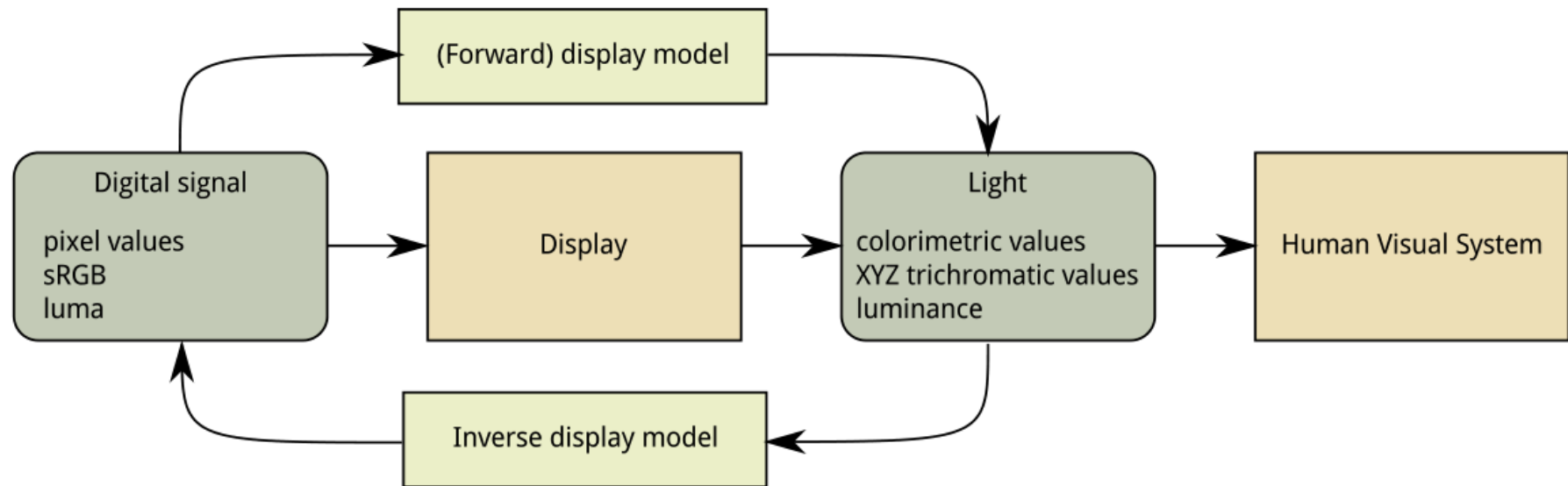
Display model

[Mantiuk et al., SIGGRAPH 2008]

# Display model, luminance and luma

# Forward and inverse display model

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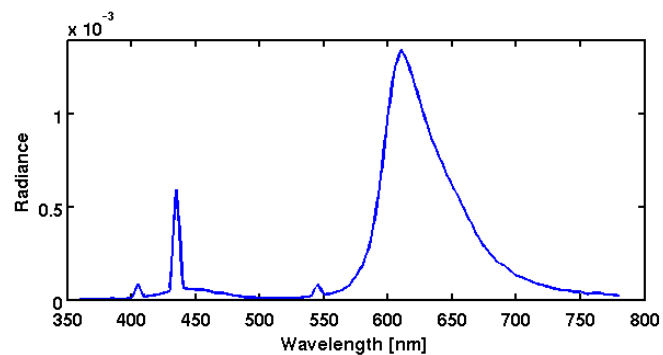
# Luminance

- ▶ Luminance – perceived brightness of light, adjusted for the sensitivity of the visual system to wavelengths

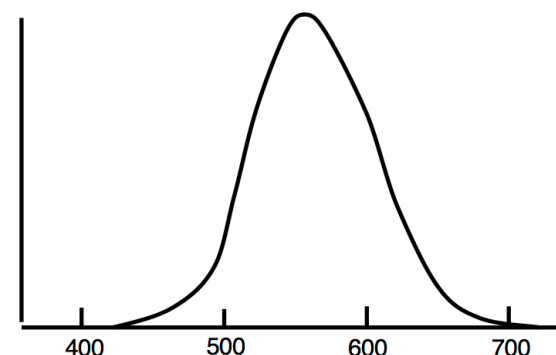
Luminance

$$L_V = \int_0^{\infty} L(\lambda) \cdot V(\lambda) d\lambda$$

Light spectrum (radiance)



Luminous efficiency function (weighting)



# Luminance and Luma

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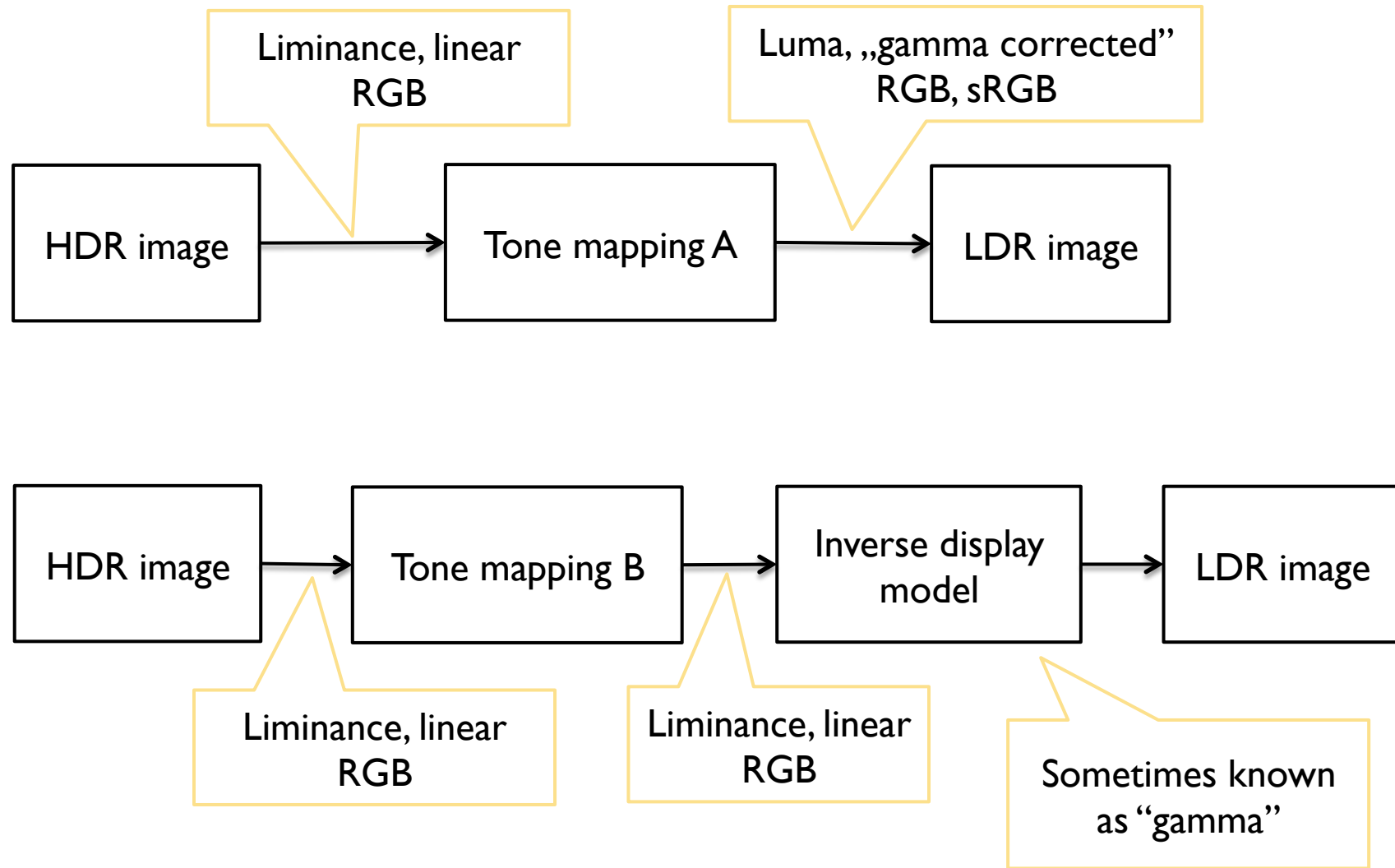
## ▶ Luminance

- ▶ Photometric quantity defined by the spectral luminous efficiency function
- ▶  $L \approx 0.2126 R + 0.7152 G + 0.0722 B$
- ▶ Units:  $\text{cd}/\text{m}^2$

## ▶ Luma

- ▶ Gray-scale value computed from LDR (gamma corrected) image
- ▶  $Y = 0.2126 R' + 0.7152 G' + 0.0722 B'$
- ▶ Unitless

# Two ways to do tone-mapping

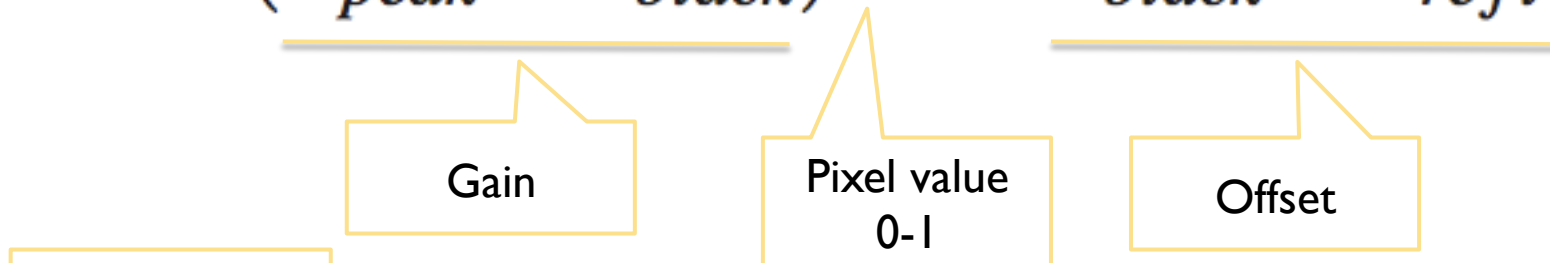


# (Forward) Display model

## ► GOG: Gain-Gamma-Offset



$$L = (L_{peak} - L_{black}) V^\gamma + L_{black} + L_{refl}$$



Reflectance factor (0.01)

$$L_{refl} = \frac{k}{2\pi} E_{amb}$$

Ambient illumination (in lux)

# Inverse display model

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Symbols are the same as for the forward display model

$$V = \left( \frac{L - L_{black} - L_{refl}}{L_{peak} - L_{black}} \right)^{(1/\gamma)}$$

Note: This display model does not address any colour issues. The same equation is applied to red, green and blue color channels. The assumption is that the display primaries are the same as for the sRGB color space.



# Arithmetic of HDR images

# Arithmetic of HDR images

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- ▶ How does the basic arithmetic operations
  - ▶ Addition
  - ▶ Multiplication
  - ▶ Power function
- ▶ affect the appearance of an HDR image
- ▶ We work in the luminance space (NOT luma)

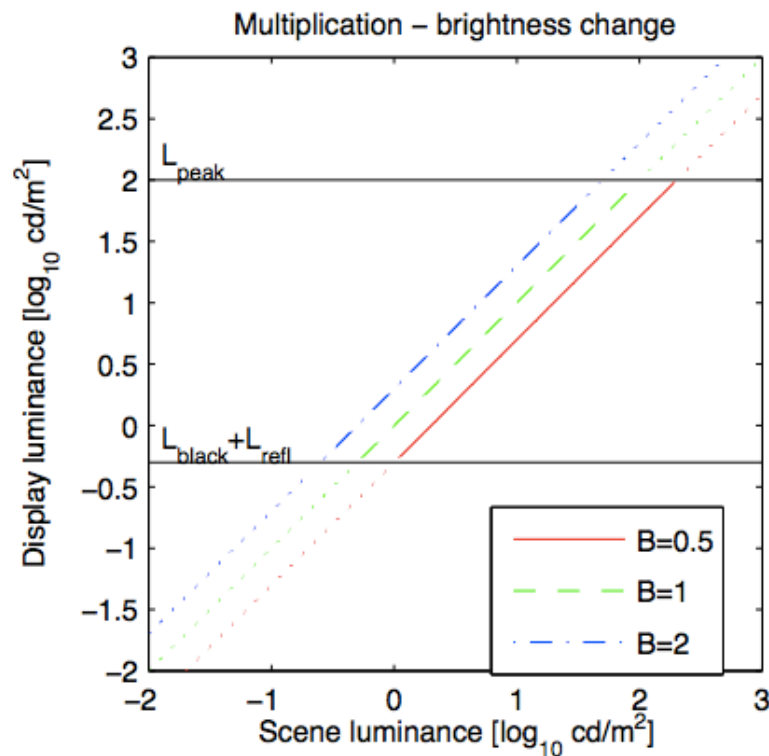
# Multiplication – brightness change

Resulting luminance

Input luminance

$$T(L_p) = B \cdot L_p$$

Brightness change parameter



- ▶ Multiplication makes the image brighter or darker
- ▶ It does not change the dynamic range!

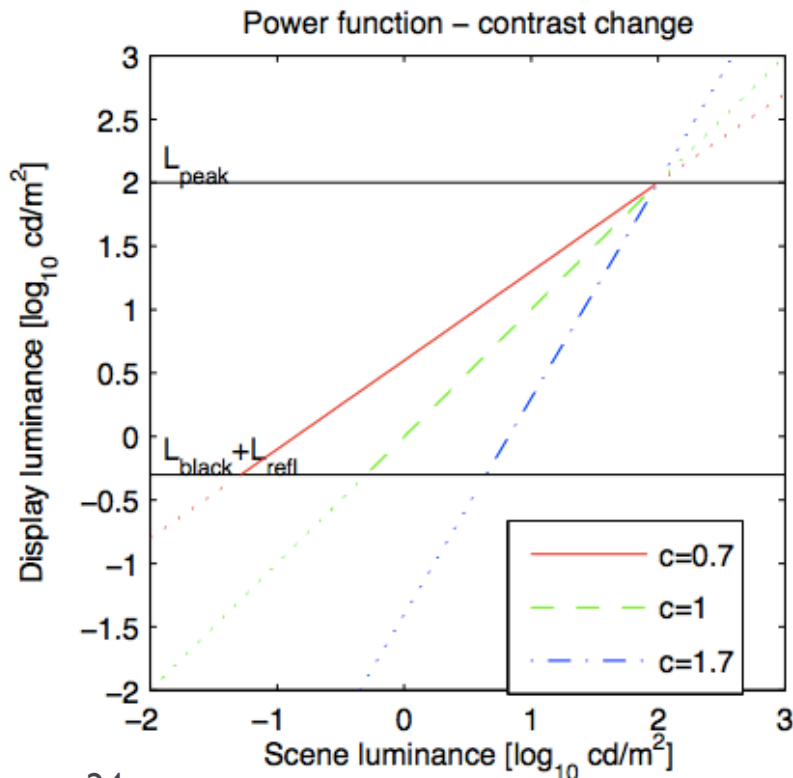
# Power function – contrast change

$$T(L_p) = \left( \frac{L_p}{L_{white}} \right)^c$$

Contrast change  
(gamma)

Luminance of  
white

- ▶ Power function stretches or shrinks image dynamic range
- ▶ It is usually performed relative to reference white
- ▶ Apparent brightness changes is the side effect of pushing tones towards or away from the white point

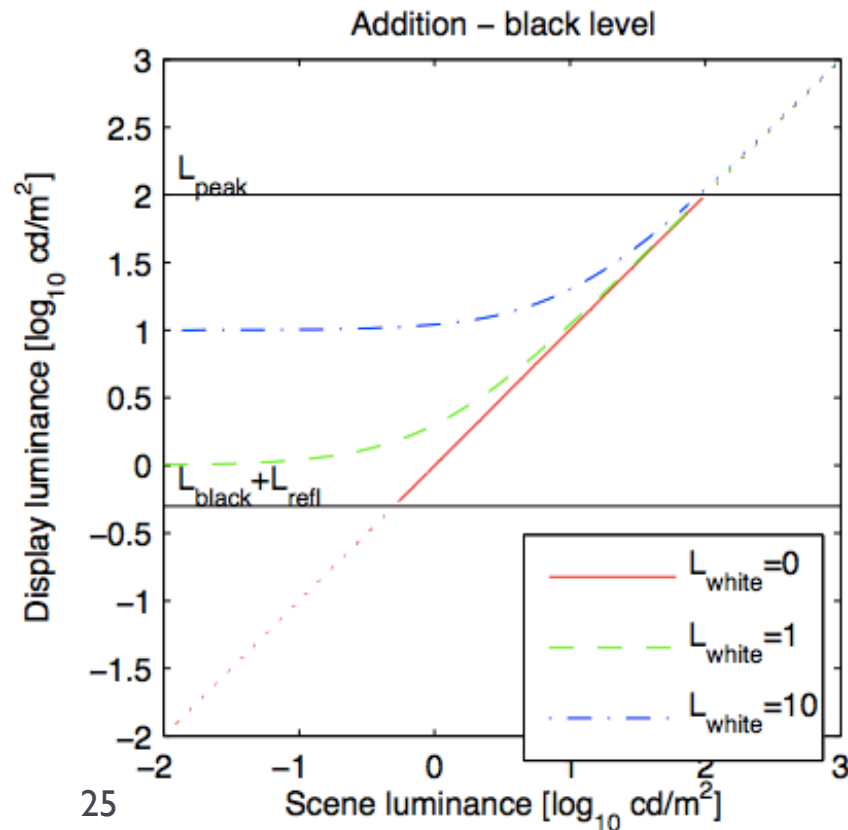


# Addition – black level

Black level (flare, fog)

$$T(L_p) = L_p + F$$

- ▶ Addition elevates black level, adds fog to an image
- ▶ It does NOT make the overall image brighter
- ▶ It reduces dynamic range



## 4 approaches to tone mapping

## 4 (major) approaches to tone mapping

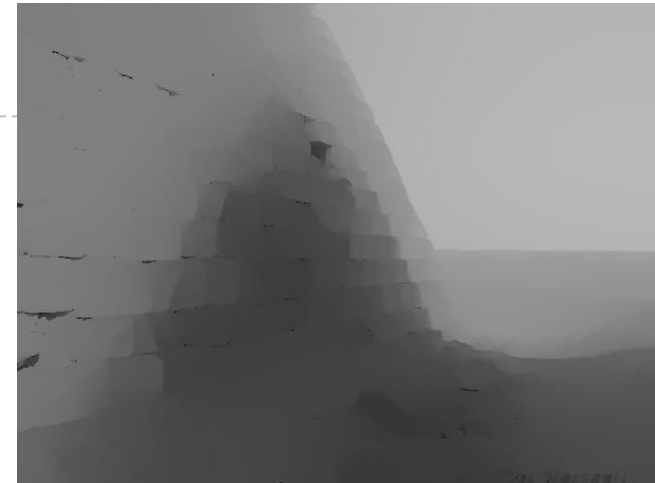
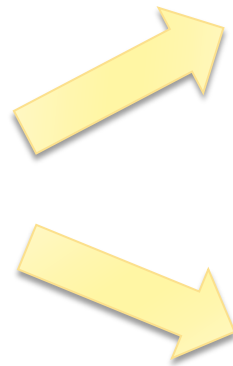
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- ▶ **Illumination & reflectance separation**
- ▶ Forward visual model
- ▶ Forward & inverse visual model
- ▶ Constrained mapping problem

# Illumination & reflectance separation



Input



Illumination



Reflectance

$$Y = I \cdot R$$

Image

Illumination

Reflectance



# Illumination and reflectance

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## Reflectance

- ▶ White  $\approx 90\%$
- ▶ Black  $\approx 3\%$
- ▶ Dynamic range  $< 100:1$
- ▶ Reflectance critical for object & shape detection

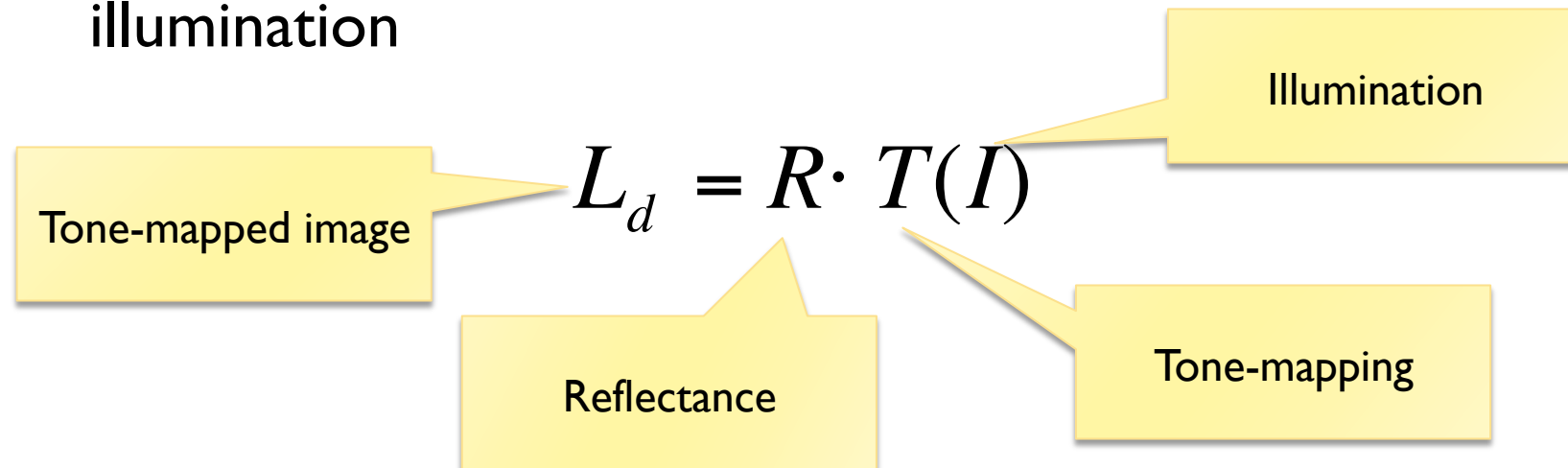
## Illumination

- ▶ Sun  $\approx 10^9 \text{ cd/m}^2$
- ▶ Lowest perceivable luminance  $\approx 10^{-6} \text{ cd/m}^2$
- ▶ Dynamic range 10,000:1 or more
- ▶ Visual system partially discounts illumination

# Reflectance & Illumination TMO

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- ▶ Hypothesis: *Distortions in reflectance are more apparent than the distortions in illumination*
- ▶ Tone mapping could preserve reflectance but compress illumination



- ▶ for example:

$$L_d = R \cdot (I / L_{white})^c \cdot L_{white}$$

# How to separate the two?

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- ▶ (Incoming) illumination – slowly changing
  - ▶ except very abrupt transitions on shadow boundaries
- ▶ Reflectance – low contrast and high frequency variations

# Gaussian filter

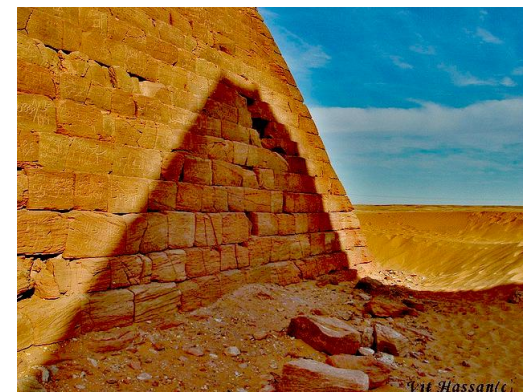
$$f(x) = \frac{1}{2\pi\sigma_s} e^{\frac{-x^2}{2\sigma_s^2}}$$

- ▶ First order approximation



- ▶ Blurs sharp boundaries
- ▶ Causes halos

Tone mapping  
result



# Bilateral filter

$$I_p \approx \frac{1}{k_s} \sum_{t \in \Omega} f(p-t) g(L_p - L_t) L_p$$

- ▶ Better preserves sharp edges



Tone mapping result

- ▶ Still some blurring on the edges
- ▶ Reflectance is not perfectly separated from illumination near edges



[Durand & Dorsey, SIGGRAPH 2002]

# WLS filter

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## ▶ Weighted-least-squares optimization

Make reconstructed image  $u$   
possibly close to input  $g$

Smooth out the image by making  
partial derivatives close to 0

$$\sum_p \left( (u_p - g_p)^2 + \lambda \left( a_{x,p}(g) \left( \frac{\partial u}{\partial x} \right)_p^2 + a_{y,p}(g) \left( \frac{\partial u}{\partial y} \right)_p^2 \right) \right) \rightarrow \min$$

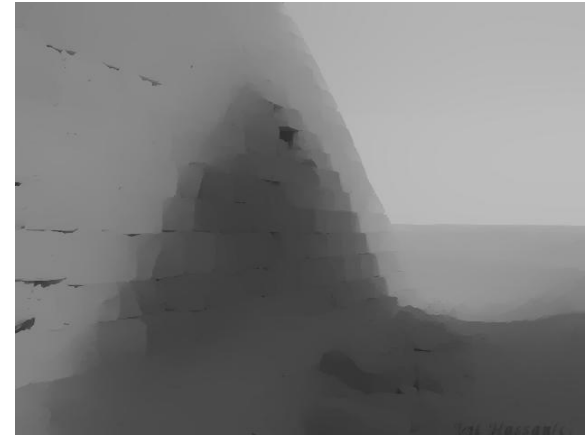
Spatially varying smoothing – less  
smoothing near the edges

## ▶ [Farbman et al., SIGGRAPH 2008]

# WLS filter

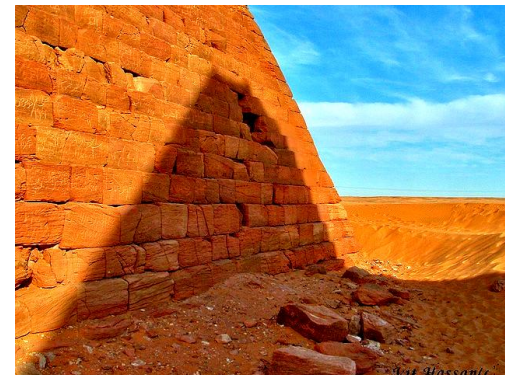
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- ▶ Stronger smoothing and still distinct edges



Tone mapping result

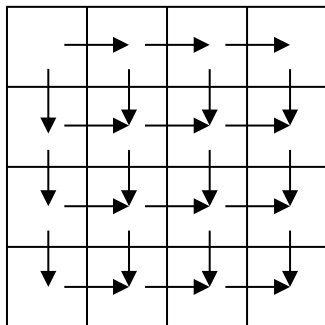
- ▶ Can produce stronger effects with fewer artifacts



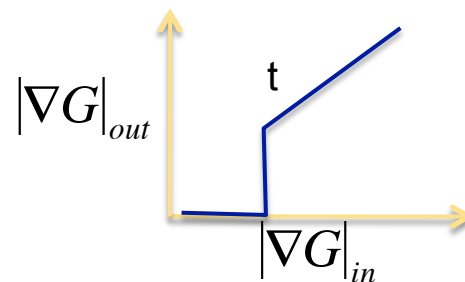
# Retinex

- ▶ Retinex algorithm was initially intended to separate reflectance from illumination [Land 1964]
- ▶ There are many variations of Retinex, but the general principle is to eliminate from an image small gradients, which are attributed to the illumination

1 step: compute gradients in log domain



2<sup>nd</sup> step: set to 0 gradients less than the threshold



3<sup>rd</sup> step: reconstruct an image from the vector field

$$\nabla^2 I = \text{div } G$$

For example by solving the Poisson equation



# Retinex examples

From: <http://dragon.larc.nasa.gov/retinex/757/>



From: [http://www.ipol.im/pub/alg/Imps\\_retinex\\_poisson\\_equation/#ref\\_1](http://www.ipol.im/pub/alg/Imps_retinex_poisson_equation/#ref_1)

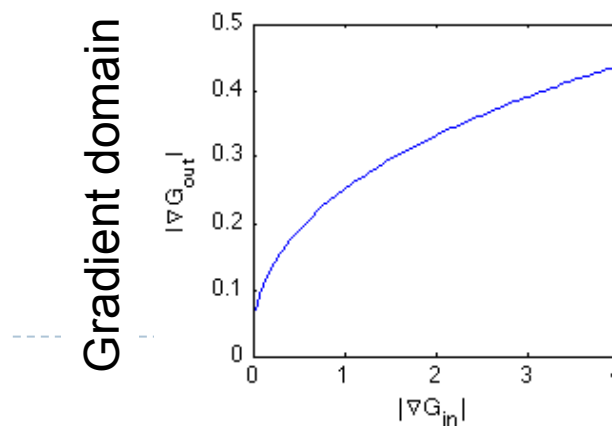
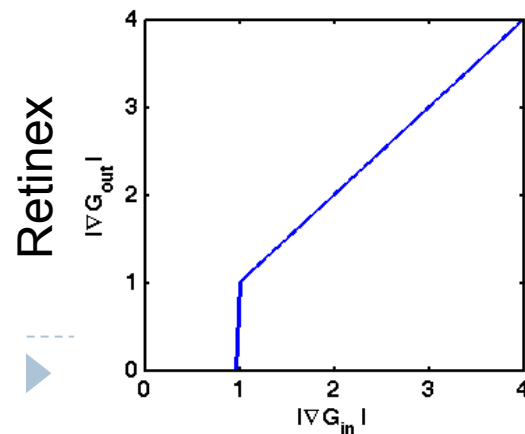


# Gradient domain HDR compression



[Fattal et al.,  
SIGGRAPH 2002]

- ▶ Similarly to Retinex, it operates on log-gradients
- ▶ But the function amplifies small contrast instead of removing it



- Contrast compression achieved by global contrast reduction
  - Enhance reflectance, then compress everything

## 4 (major) approaches to tone mapping

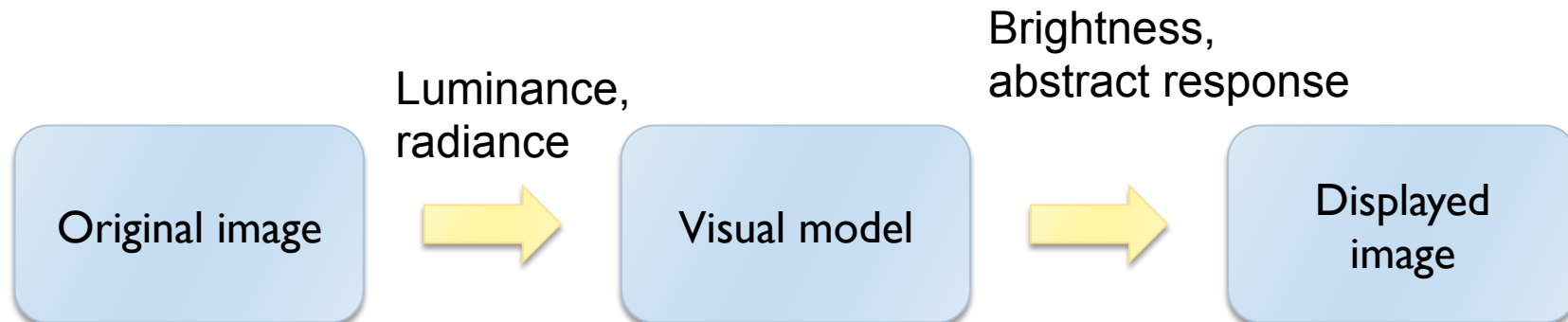
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- ▶ Illumination & reflectance separation
- ▶ **Forward visual model**
- ▶ Forward & inverse visual model
- ▶ Constrained mapping problem

# Forward visual model

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- ▶ Mimic the processing in the human visual system



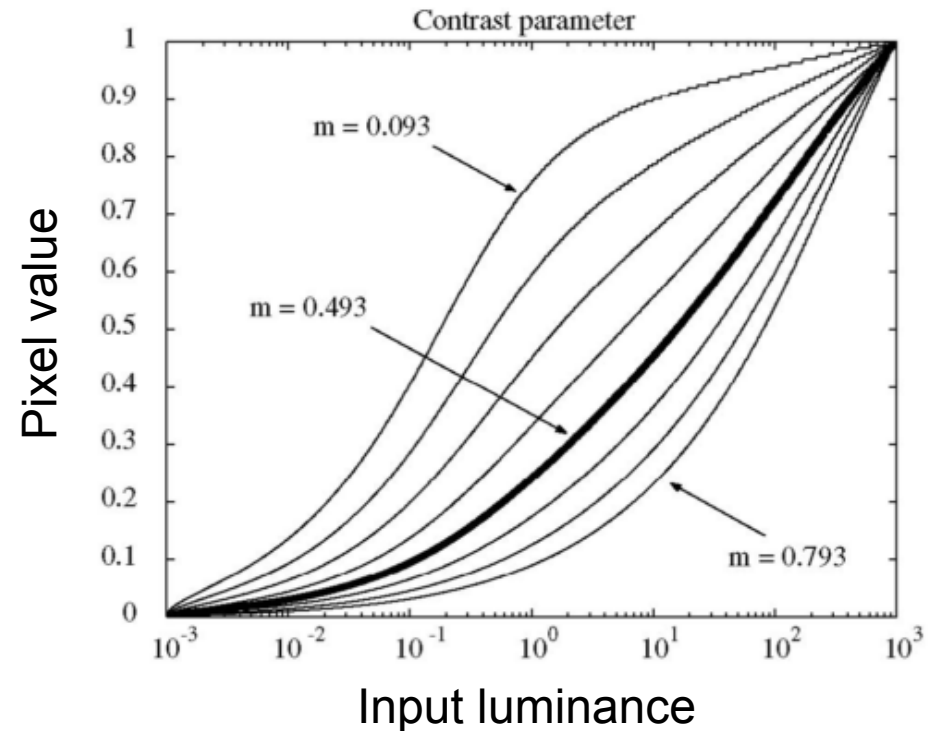
- ▶ Assumption: what is displayed is brightness or abstract response of the visual system
- ▶ Problem: double processing

# Photoreceptor response

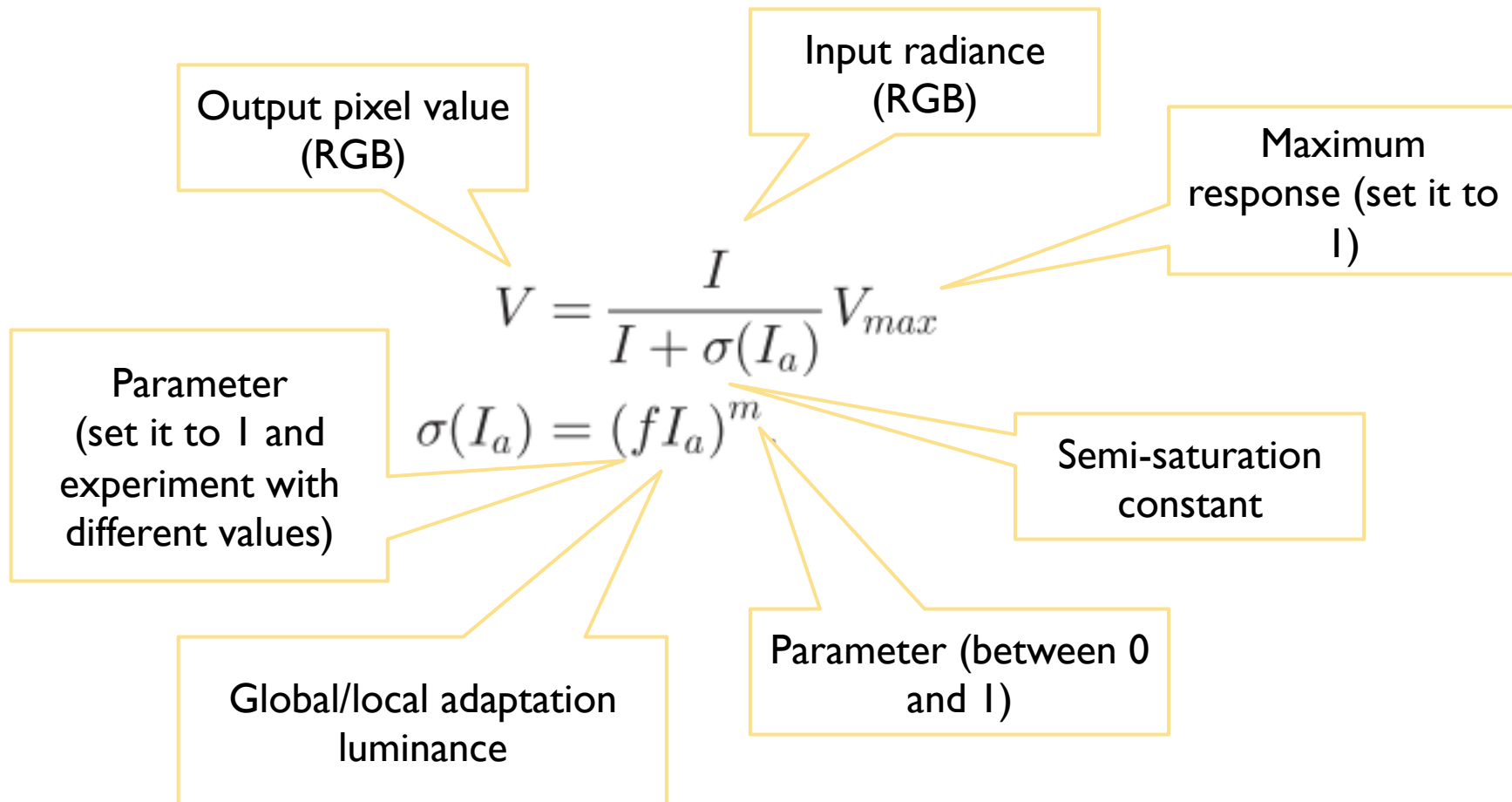
- ▶ Dynamic range reduction inspired by photoreceptor physiology
  - ▶ [Reinhard & Devlin '05]

$$V = \frac{I}{I + \sigma(I_a)} V_{max}$$
$$\sigma(I_a) = (fI_a)^m.$$

- ▶ From gamma to sigmoidal response:



# Photoreceptor TMO





# Results: photoreceptor TMO



Our operator



Bilateral filtering



Trilateral filtering



Histogram adjustment



Photographic tonemapping (global)



Photographic tonemapping (local)



Logarithmic mapping



Adaptive logarithmic mapping



Ashikhmin's operator



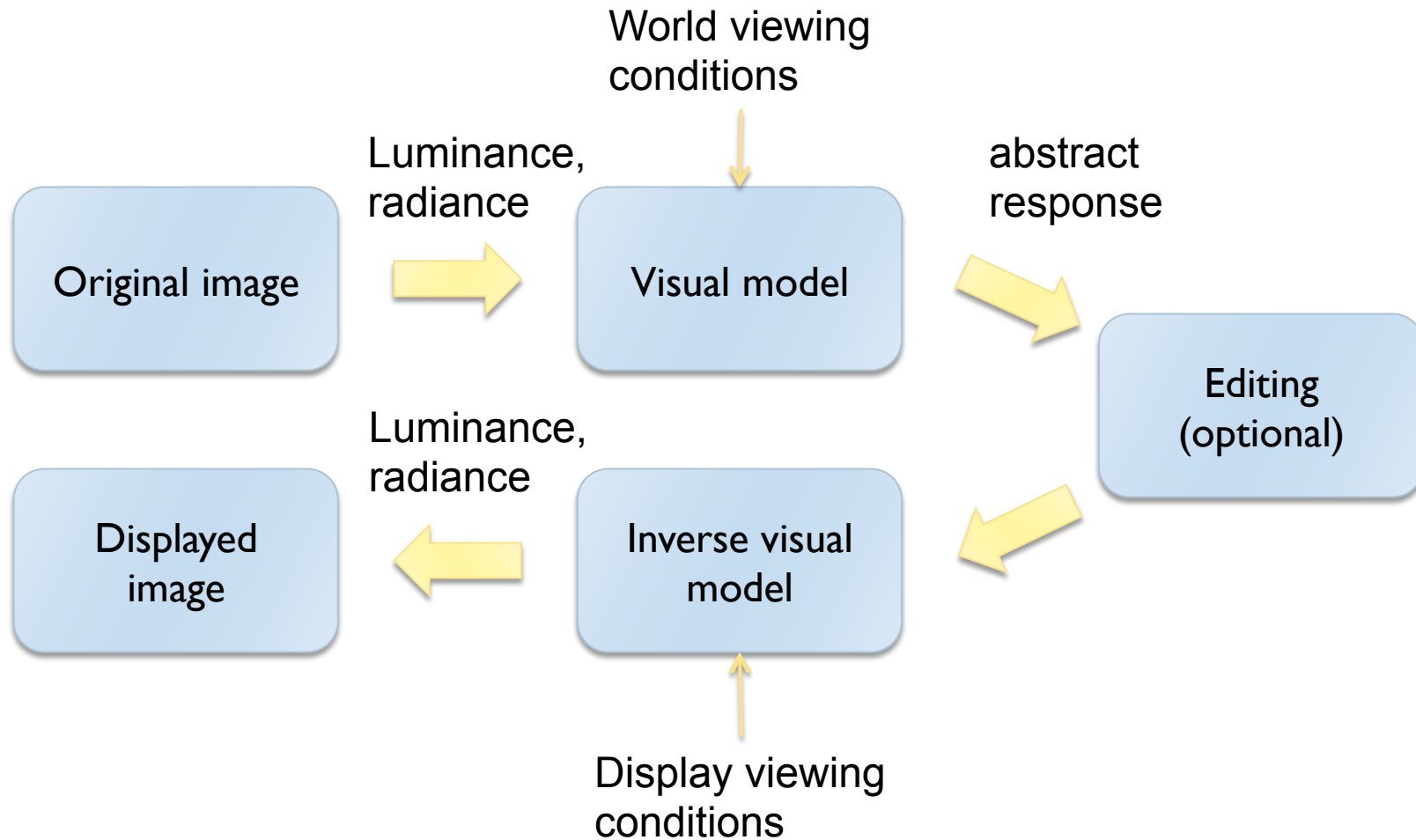
## 4 (major) approaches to tone mapping

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- ▶ Illumination & reflectance separation
- ▶ Forward visual model
- ▶ **Forward & inverse visual model**
- ▶ Constrained mapping problem

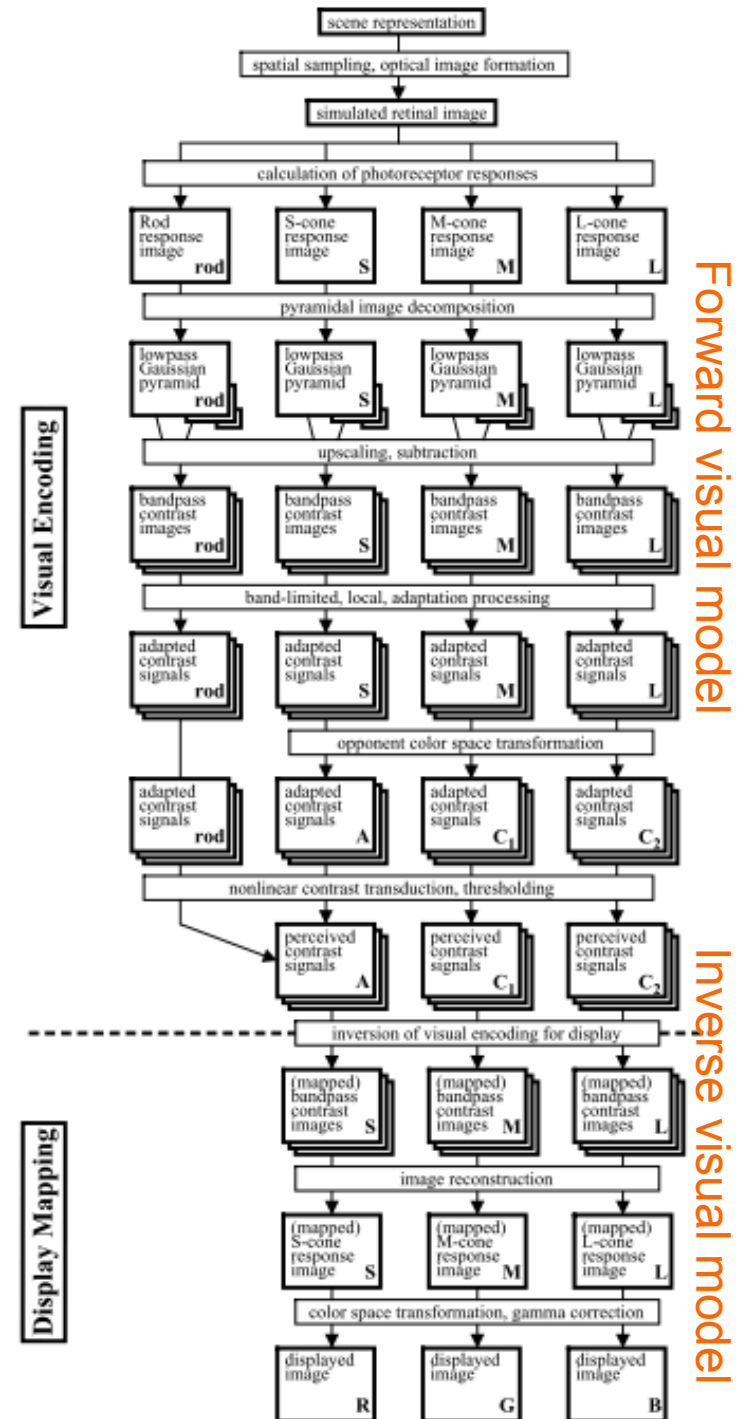
# Forward and inverse visual model

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# Multi-scale model

- ▶ Multi-scale model of adaptation and spatial vision and color appearance
  - ▶ [Pattanaik et al. '98]
- ▶ Combines
  - ▶ psychophysical threshold and superthreshold visual models
  - ▶ light & dark adaptation models
  - ▶ Hunt's color appearance model
- ▶ One of the most sophisticated visual models



# Forward and inverse visual model

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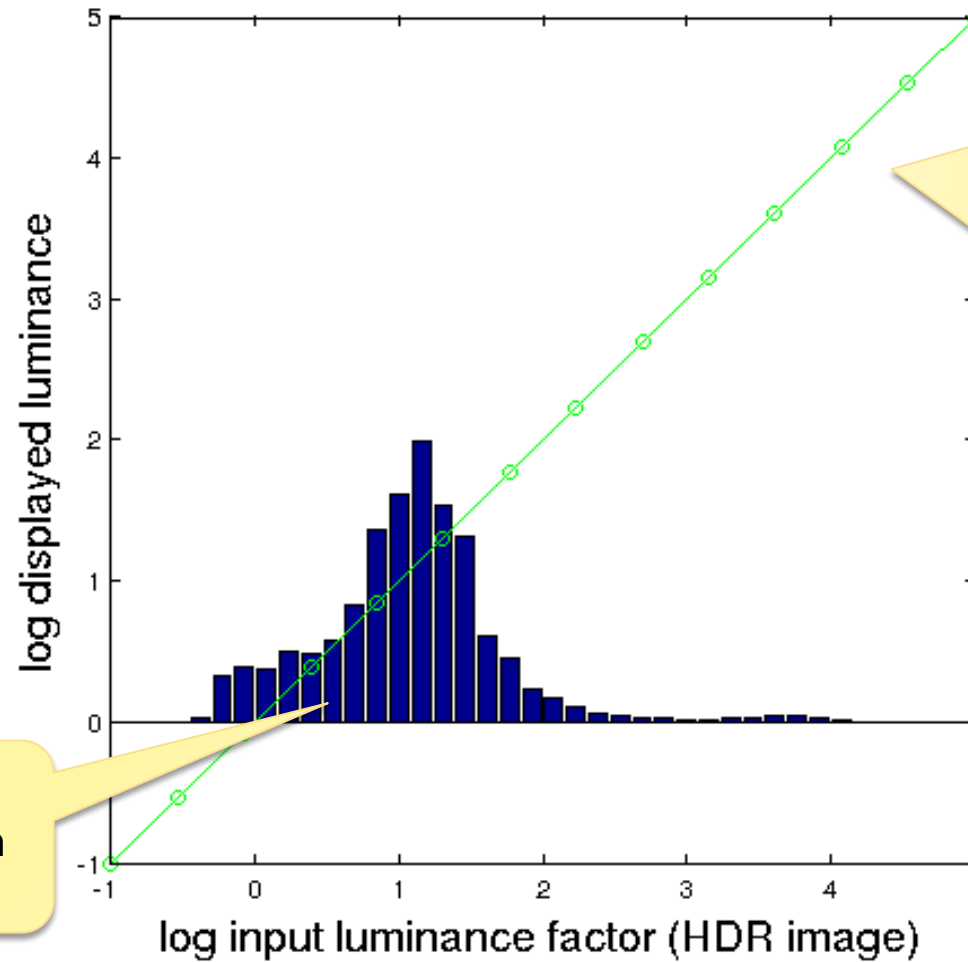
- ▶ **Advantages of F&I visual models**
  - ▶ Can render images for different viewing conditions
    - ▶ Different state of chromatic or luminance adaptation
  - ▶ Physically plausible
    - ▶ output in the units of luminance or radiance
- ▶ **Shortcomings F&I visual models**
  - ▶ Assume that a standard display can reproduce the impression of viewing much brighter or darker scenes
  - ▶ Cannot ensure that the resulting image is within the dynamic range of the display
    - ▶ Not necessary meant to reduce the dynamic range
  - ▶ Visual models are difficult to invert

## 4 (major) approaches to tone mapping

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- ▶ Illumination & reflectance separation
- ▶ Forward visual model
- ▶ Forward & inverse visual model
- ▶ **Constrained mapping problem**

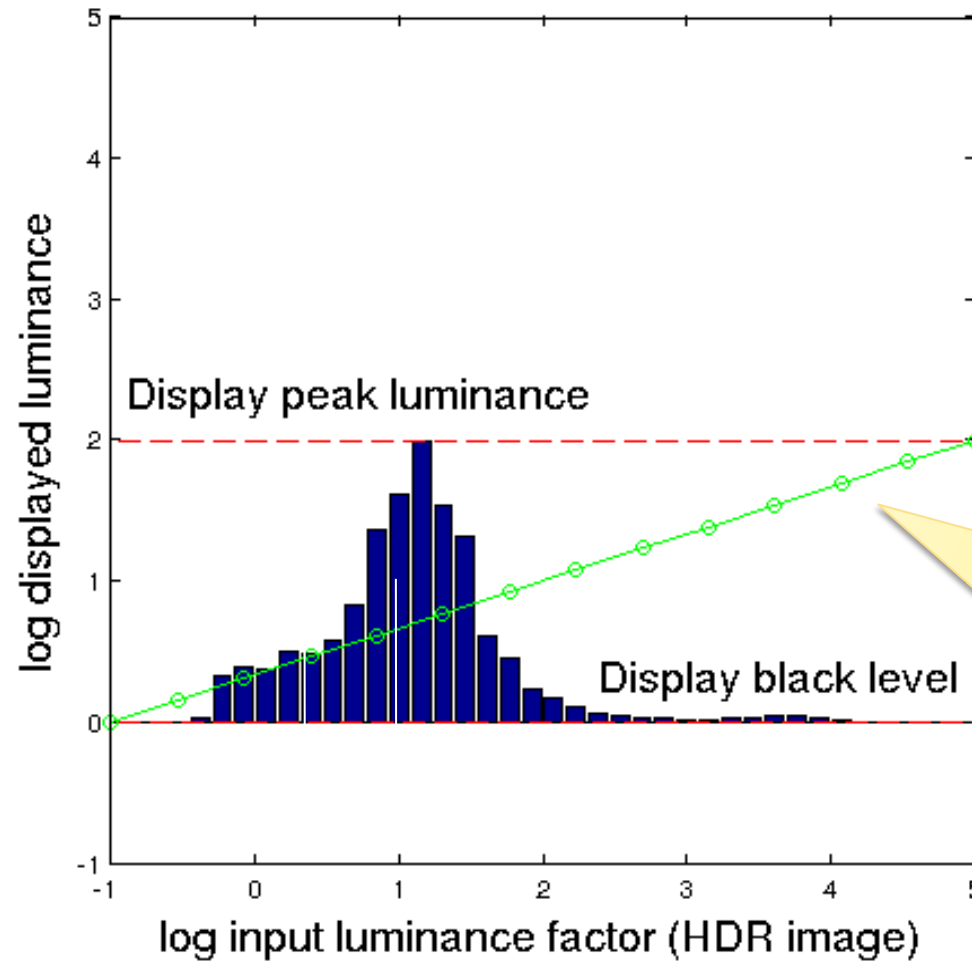
# Global tone mapping operator



Best tone-mapping is the one which does not do anything, i.e. slope of the tone-mapping curves is equal to 1.

Image histogram

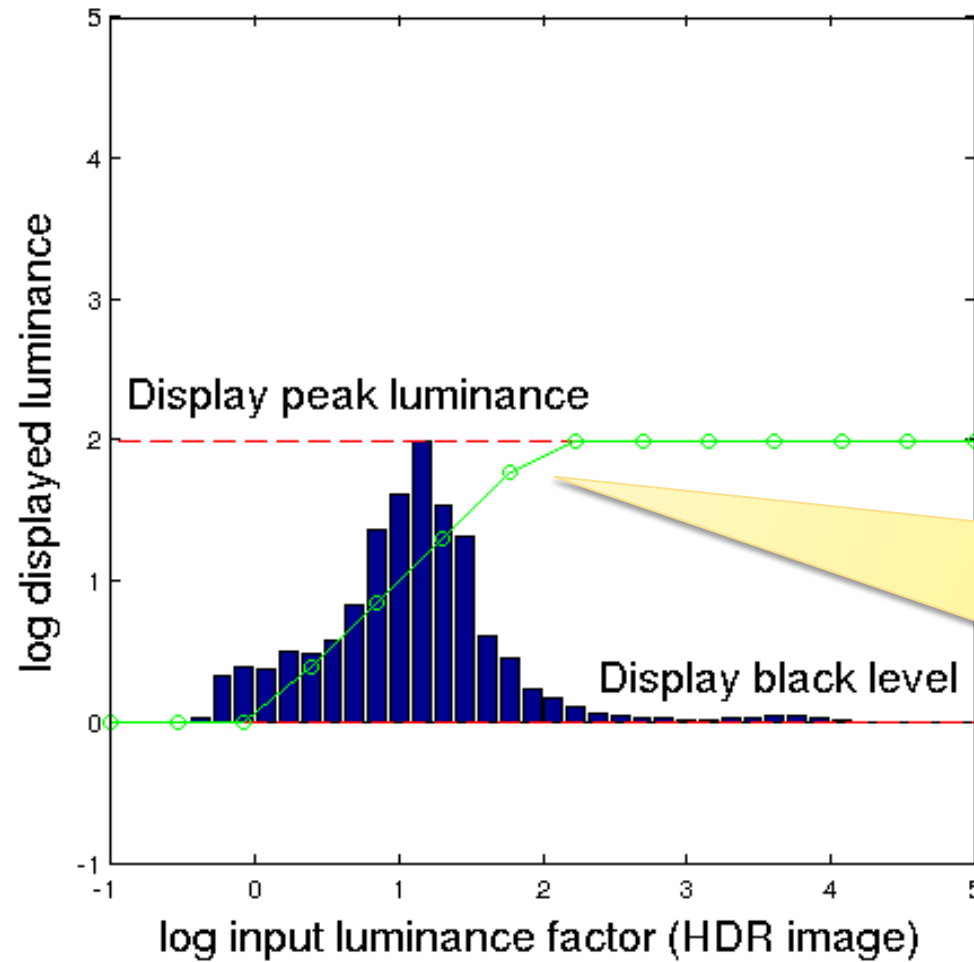
# Display limitations



But in practice contrast (slope) must be limited due to display limitations.



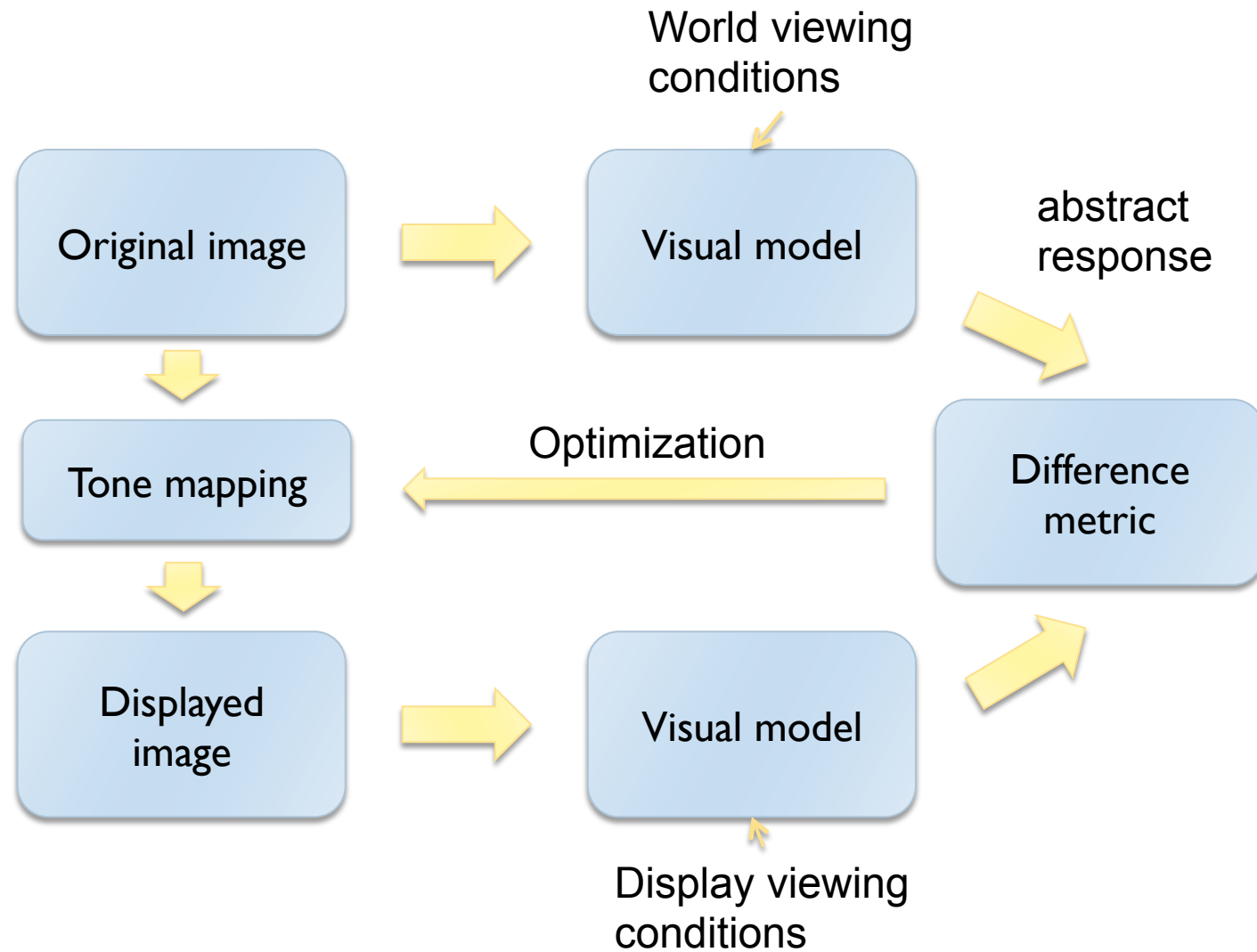
# Tone mapping



Global tone-mapping is a compromise between clipping and contrast compression.

# Constrained mapping + visual models

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## 4 (major) approaches to tone mapping

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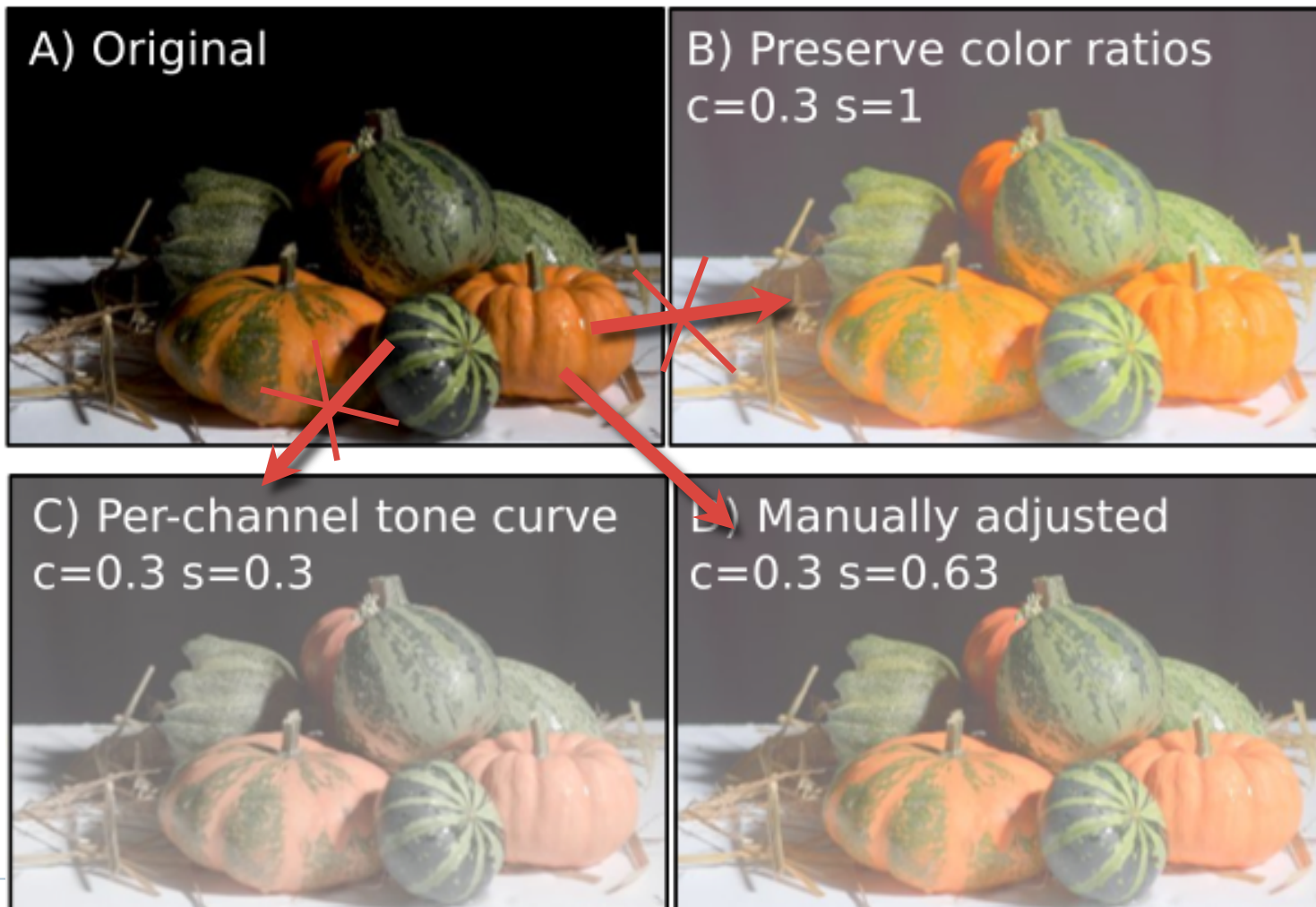
- ▶ Illumination & reflectance separation
- ▶ Forward visual model
- ▶ Forward & inverse visual model
- ▶ Constrained mapping problem



Color

# Motivation

To preserve the appearance of color after tone mapping



# Color processing

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- ▶ Existing methods
  - ▶ Apply the same processing to all color channels
    - ▶ works for simple (global) TMOs
  - ▶ **Operate on luminance, transfer color from the original HDR image**
  - ▶ Model color appearance



# Color processing

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- ▶ Transfer color from the original image

The diagram shows the equation  $C_{out} = \left( \frac{C_{in}}{L_{in}} \right)^s \cdot L_{out}$ . A callout box on the left points to  $C_{out}$  and is labeled "Output color channel". A callout box on the top right points to the exponent  $s$  and is labeled "Saturation parameter". A callout box on the bottom right points to  $L_{out}$  and is labeled "Resulting luminance".

$$C_{out} = \left( \frac{C_{in}}{L_{in}} \right)^s \cdot L_{out}$$

- ▶ The heuristic from Fattal et al. 2002
  - ▶ works reasonably well in practice
- ▶ **Difficulty:**
  - ▶ How to select value 's'





# Color correction for tone-mapping

Empirical formula for saturation correction  
Estimated from experimental data

[Mantiuk et al., CGF 2009]

Global contrast  
compression (gamma)

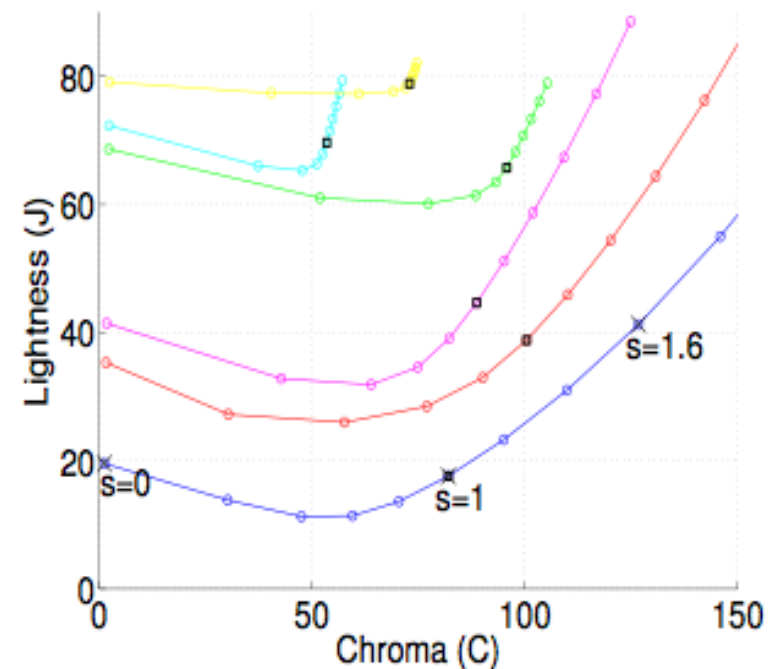
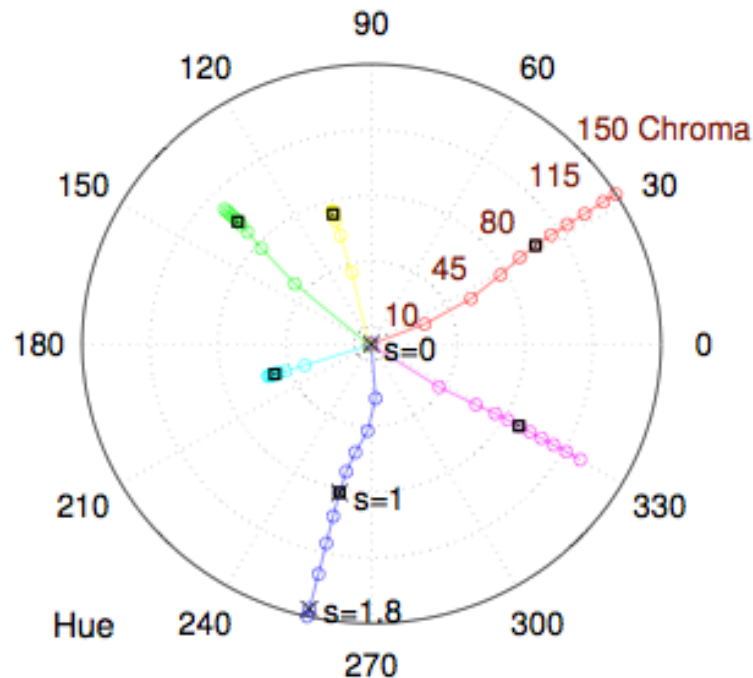
$$C_{out} = \left( \frac{C_{in}}{L_{in}} \right)^s L_{out}$$
$$s(c) = \frac{(1 + k_1) c^{k_2}}{1 + k_1 c^{k_2}}$$

$k_1=2.3892, k_2=0.8552$



# What is wrong with the color-correction formula?

$$C_{out} = \left( \frac{C_{in}}{L_{in}} \right)^s \cdot L_{out}$$



Visualization of CIECAM02 appearance correlates (hue=f(chroma), lightness=f(chroma)) for 6 sample colors.

Glare / blooming

# Glare / blooming





# Glare illusion

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"Alan Wake" © Remedy Entertainment

# Glare illusion

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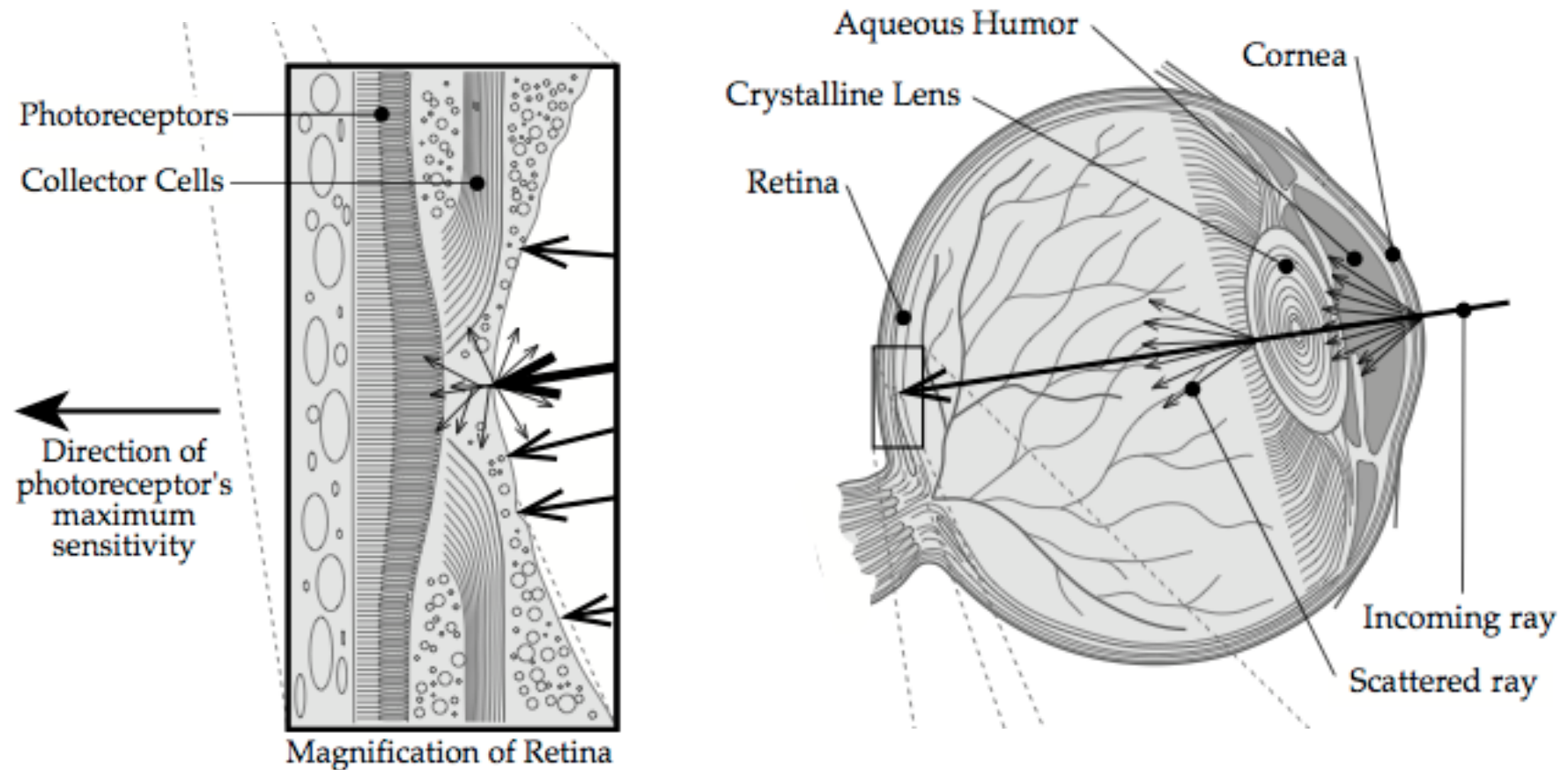
Photography



Painting



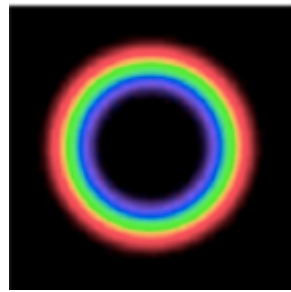
# Scattering of the light in the eye



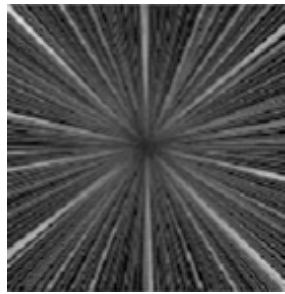
From: Sekuler, R., and Blake, R. Perception, second ed. McGraw- Hill, New York, 1990



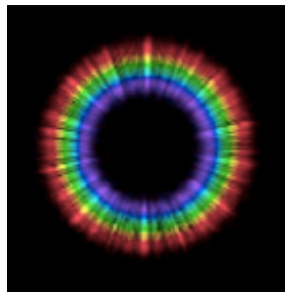
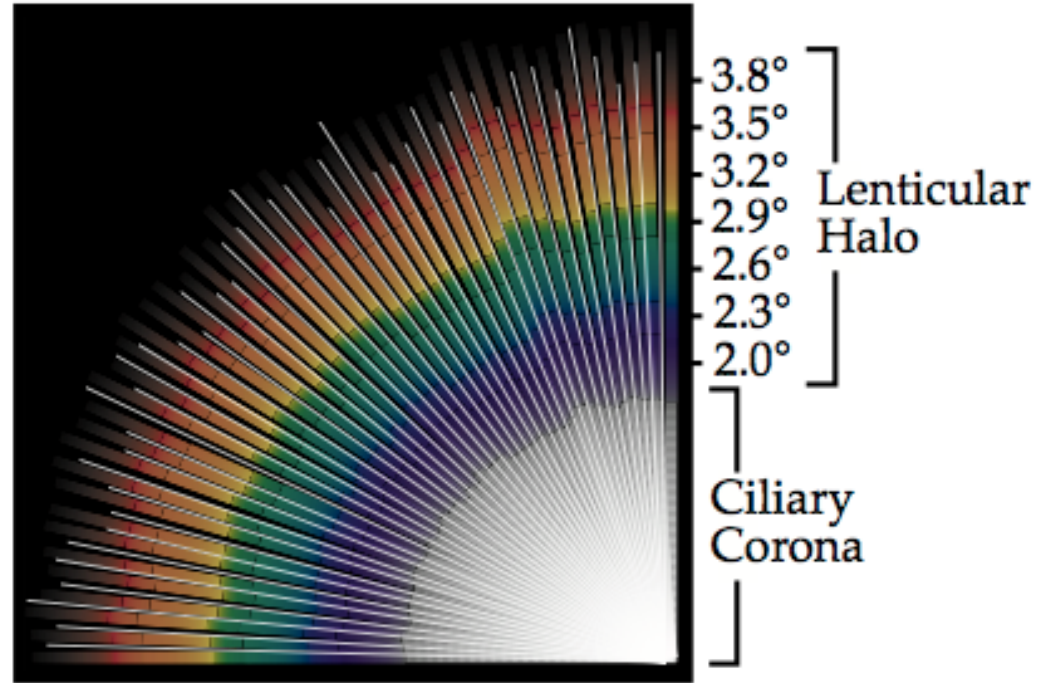
# Ciliary corona and lenticular halo



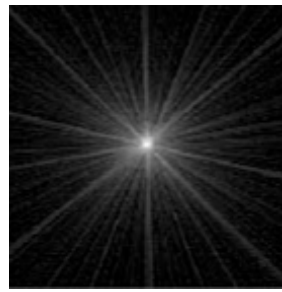
\*



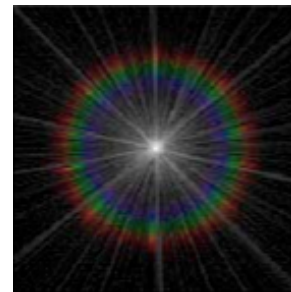
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+



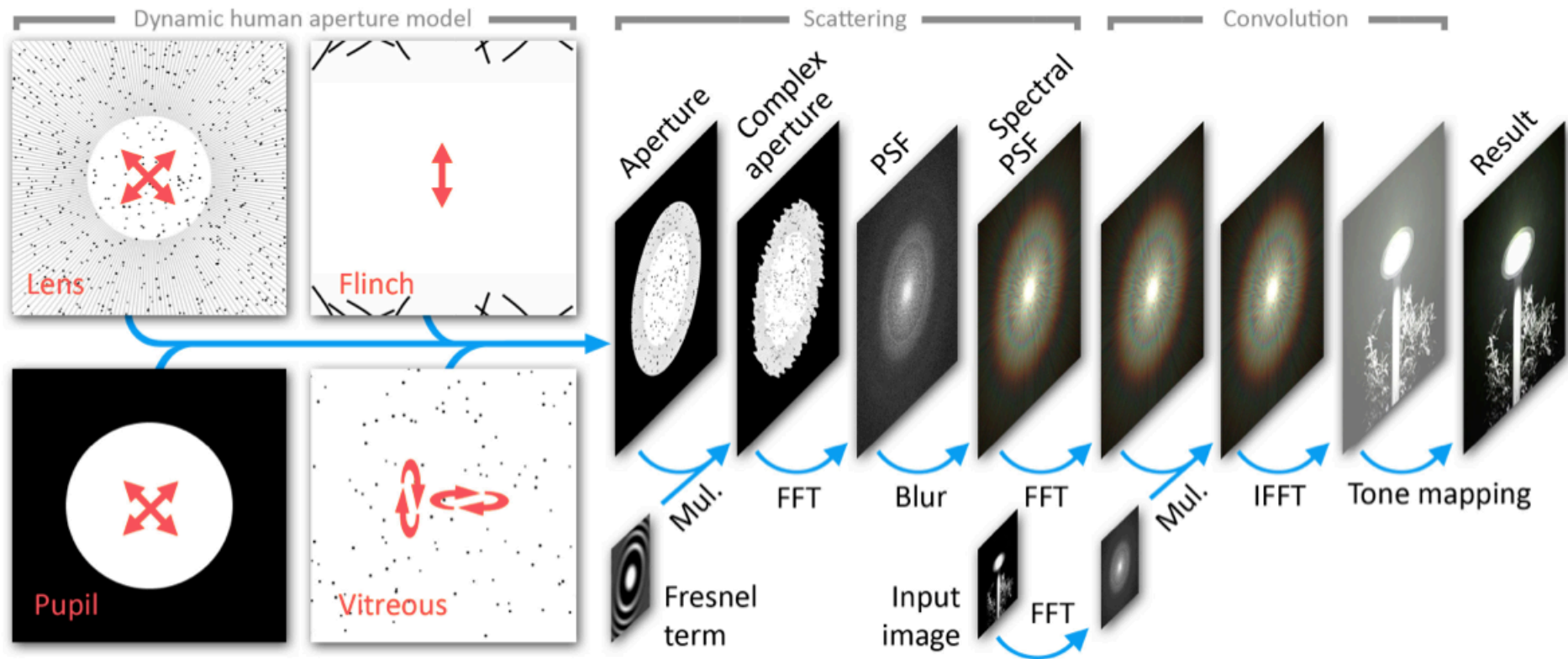
=



From: Spencer, G. et al.  
1995. Proc. of  
SIGGRAPH. (1995)



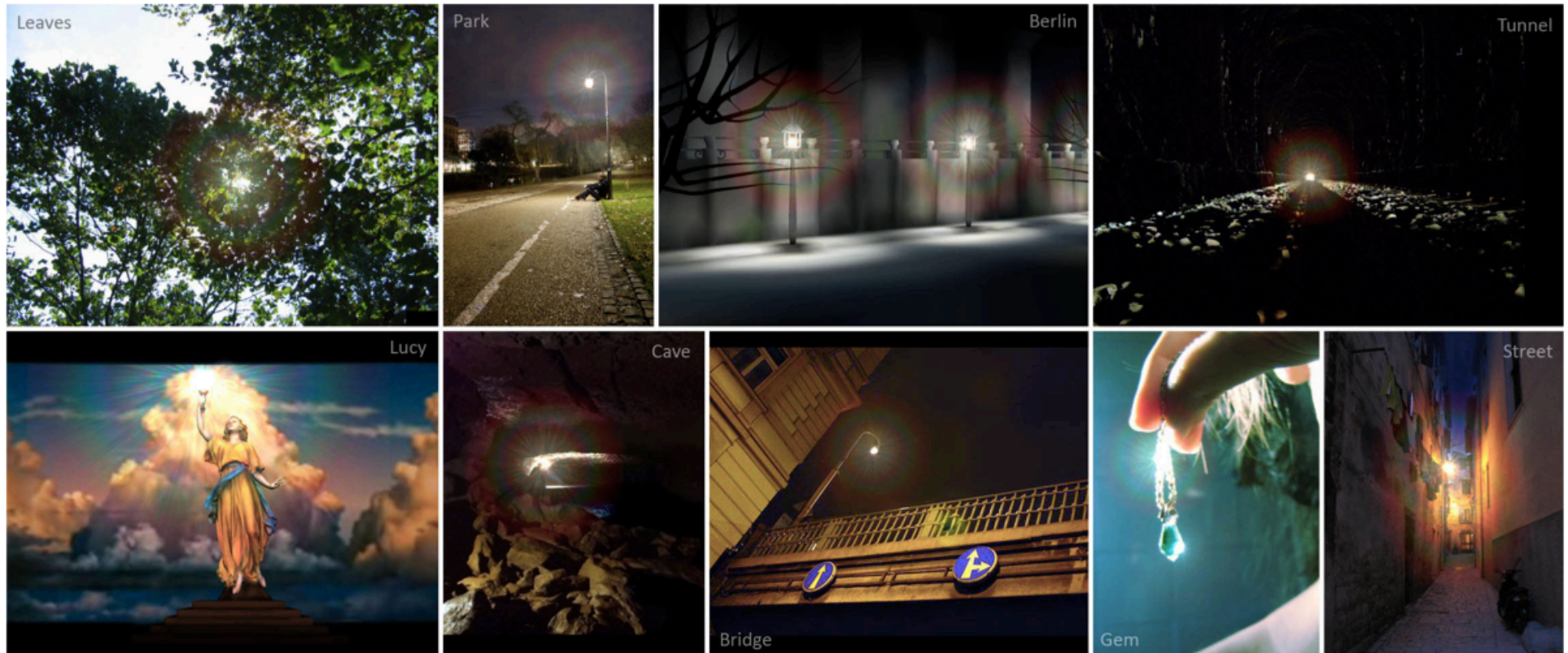
# Temporal model of glare (low level)



- ▶ The model assumes that glare is mostly caused by diffraction and scattering
- ▶ Can simulate temporal effects

# Examples of simulated glare

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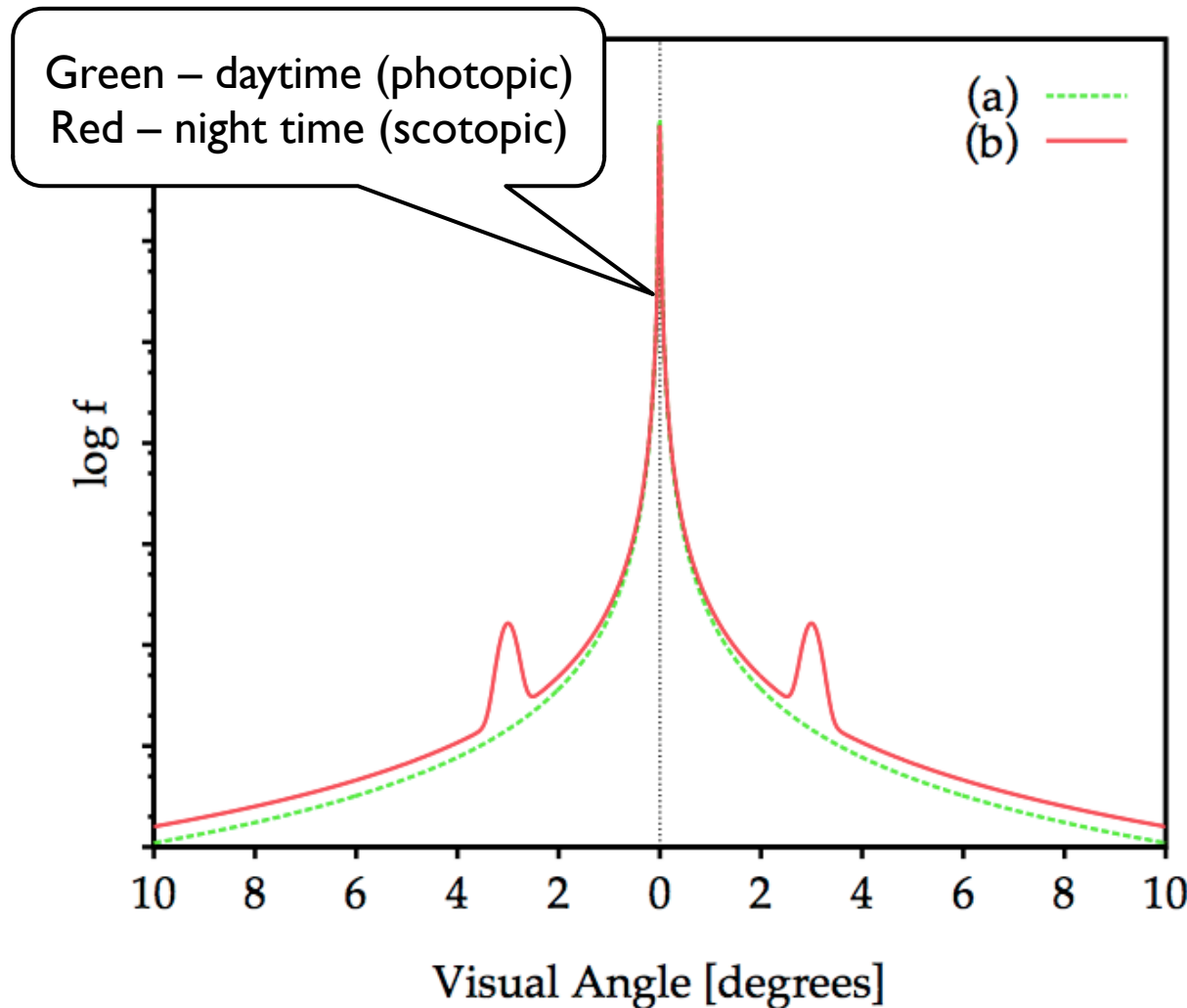
[From Ritschel et al, Eurographics 2009]

# Temporal glare

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# Point Spread Function of the eye

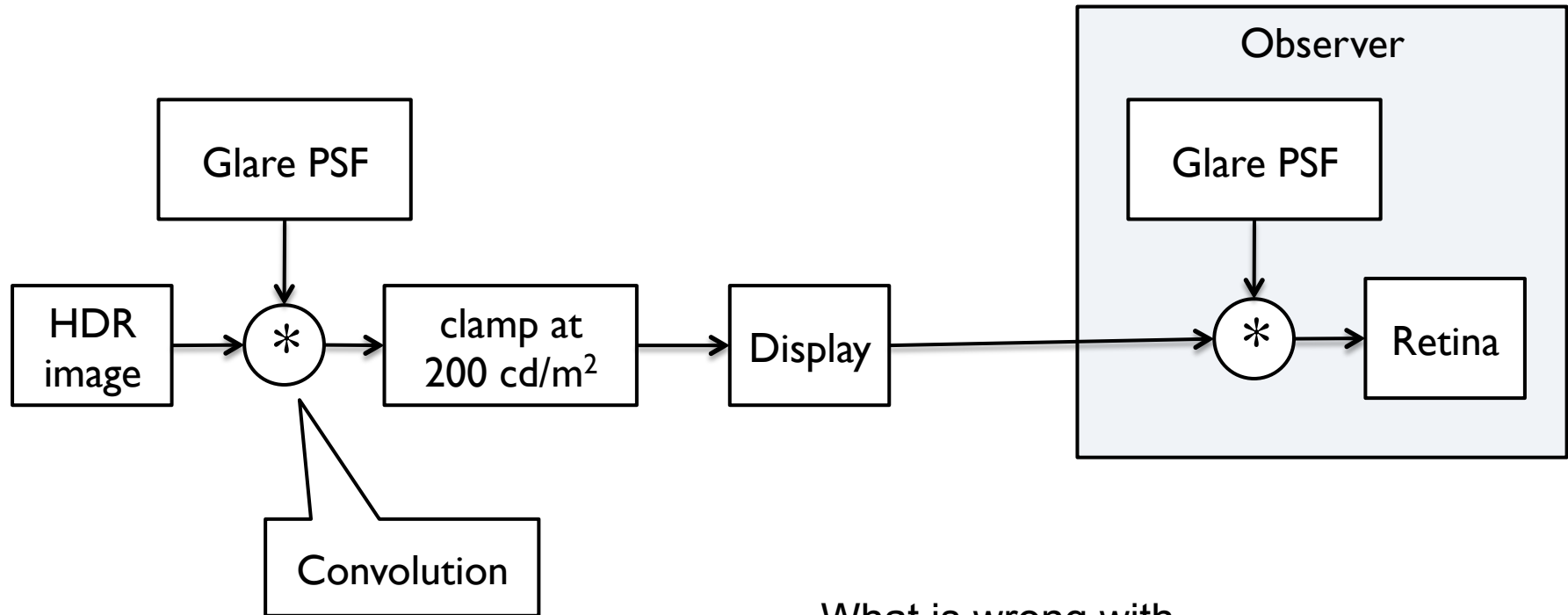


- ▶ What portion of the light is scattered towards a certain visual angle
- ▶ To simulate:
  - ▶ construct a digital filter
  - ▶ convolve the image with that filter

From: Spencer, G. et al. 1995.  
Proc. of SIGGRAPH. (1995)

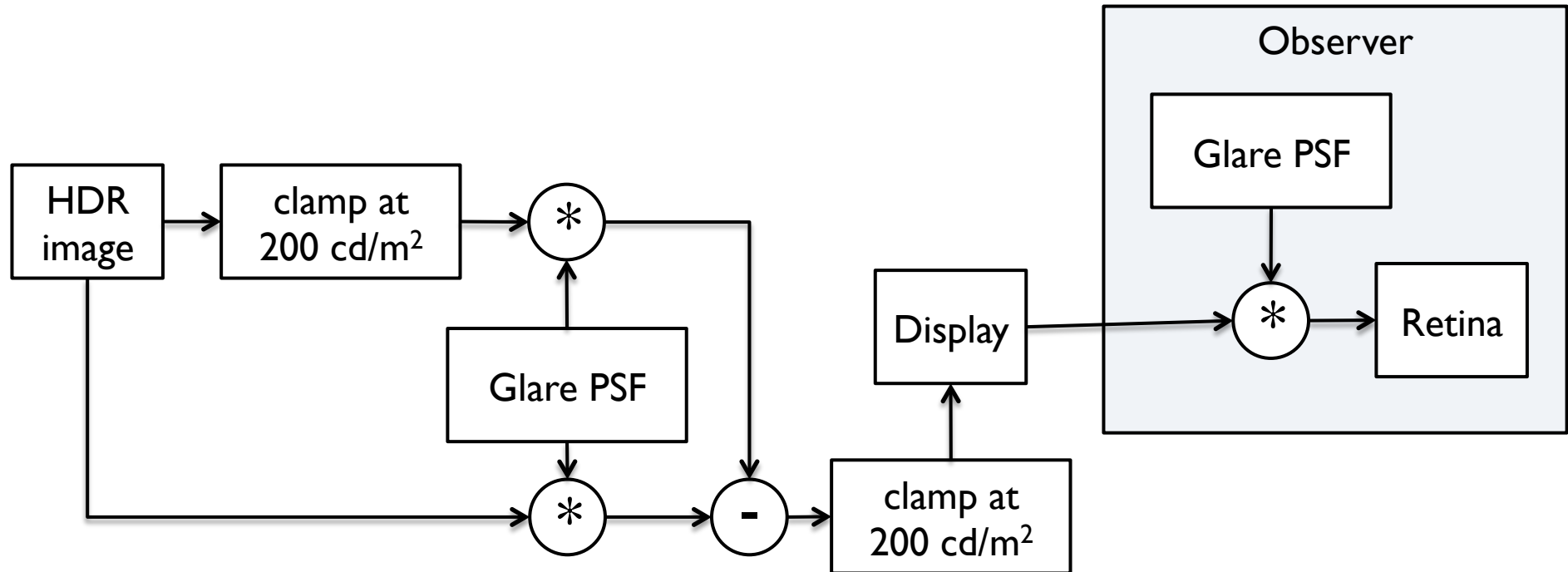


# The problem of double processing



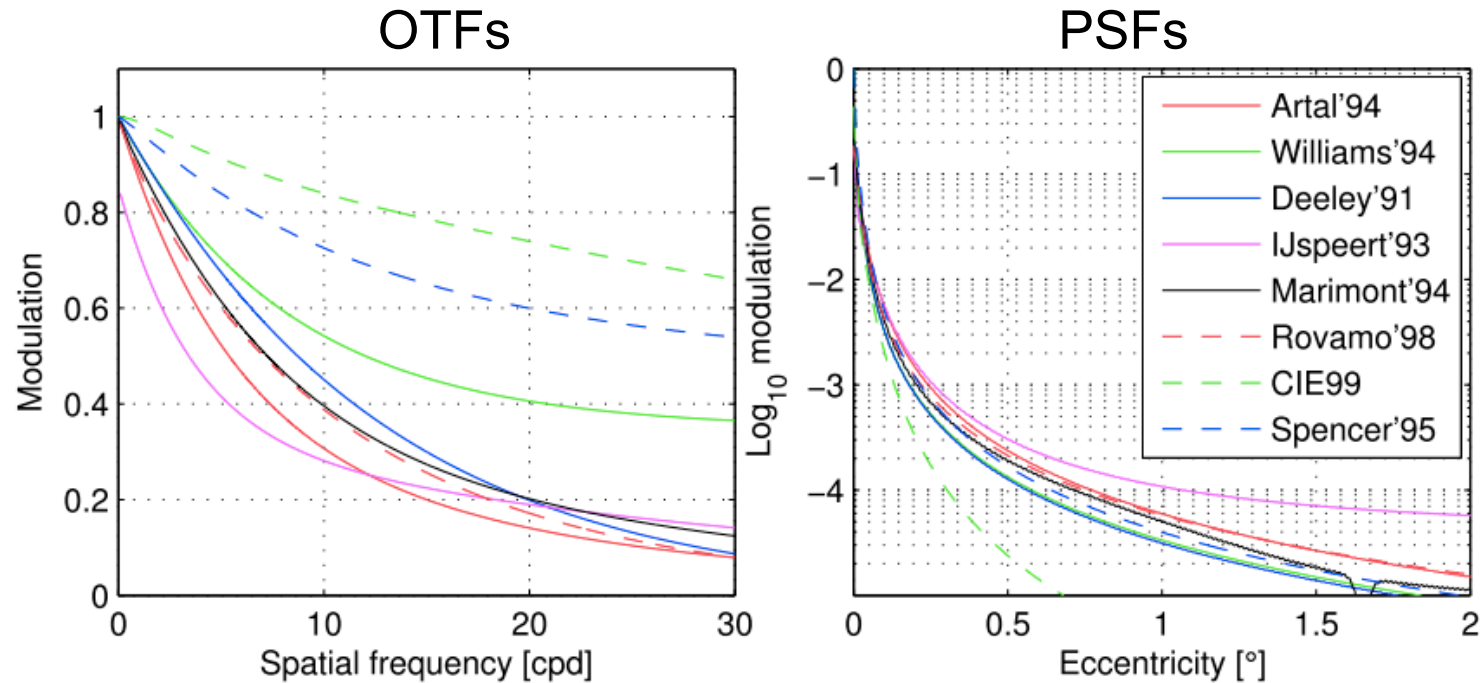
What is wrong with simulating glare this way?

# The problem of double processing



How does the diagram above avoid the problem of double processing?  
Write down the operations as equations.  
Can the processing be simplified?

# PSF vs. OTF (Optical Transfer Function)

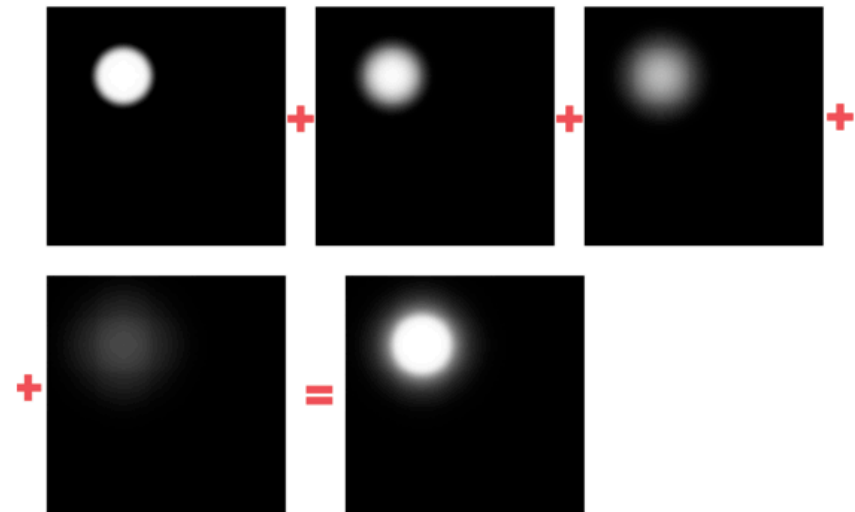


- ▶ An OTF is the Fourier transform of a PSF
- ▶ Convolution with larger kernels is faster in the Fourier domain

# Glare (or bloom) in games

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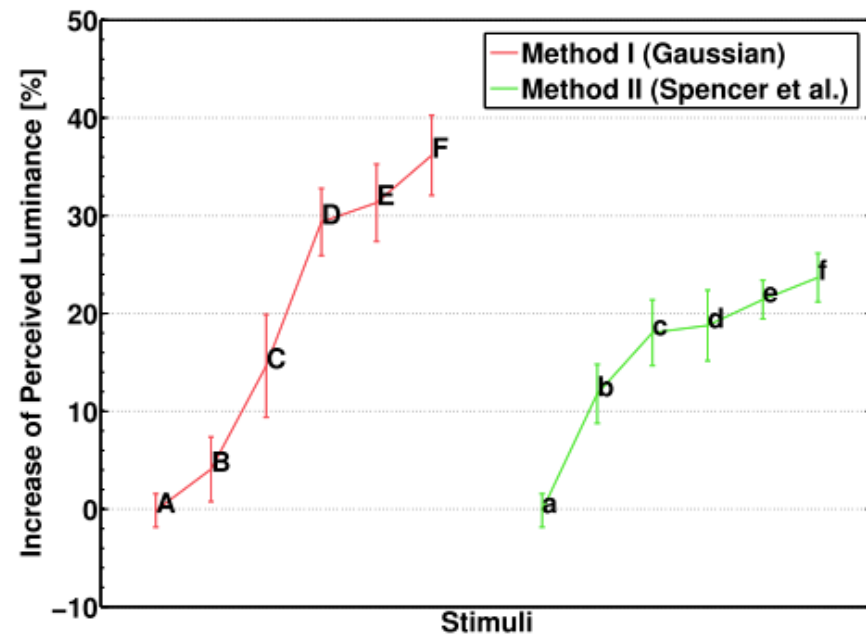
- ▶ Convolution with large, non-separable filters is too slow
- ▶ The effect is approximated by a combination of Gaussian filters
  - ▶ Each filter with different “sigma”
- ▶ The effect is meant to look good, not be an accurate model of light scattering
- ▶ Some games simulate camera rather than the eye



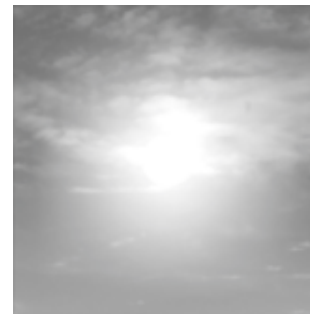


# Does the exact shape of the PSF matter?

- ▶ The illusion of increased brightness works even if the PSF is very different from the PSF of the eye



red - Gaussian



green - accurate



[Yoshida et al., APGV 2008]

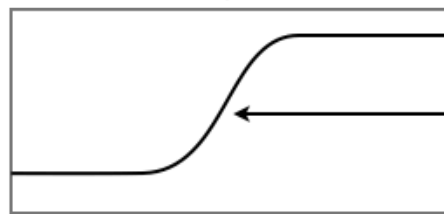
# Visual metric-driven TMOs

# Display adaptive tone-mapping

Goal: Minimize the visual difference between the input and displayed images



input scene



tone-mapping



display

argmin E

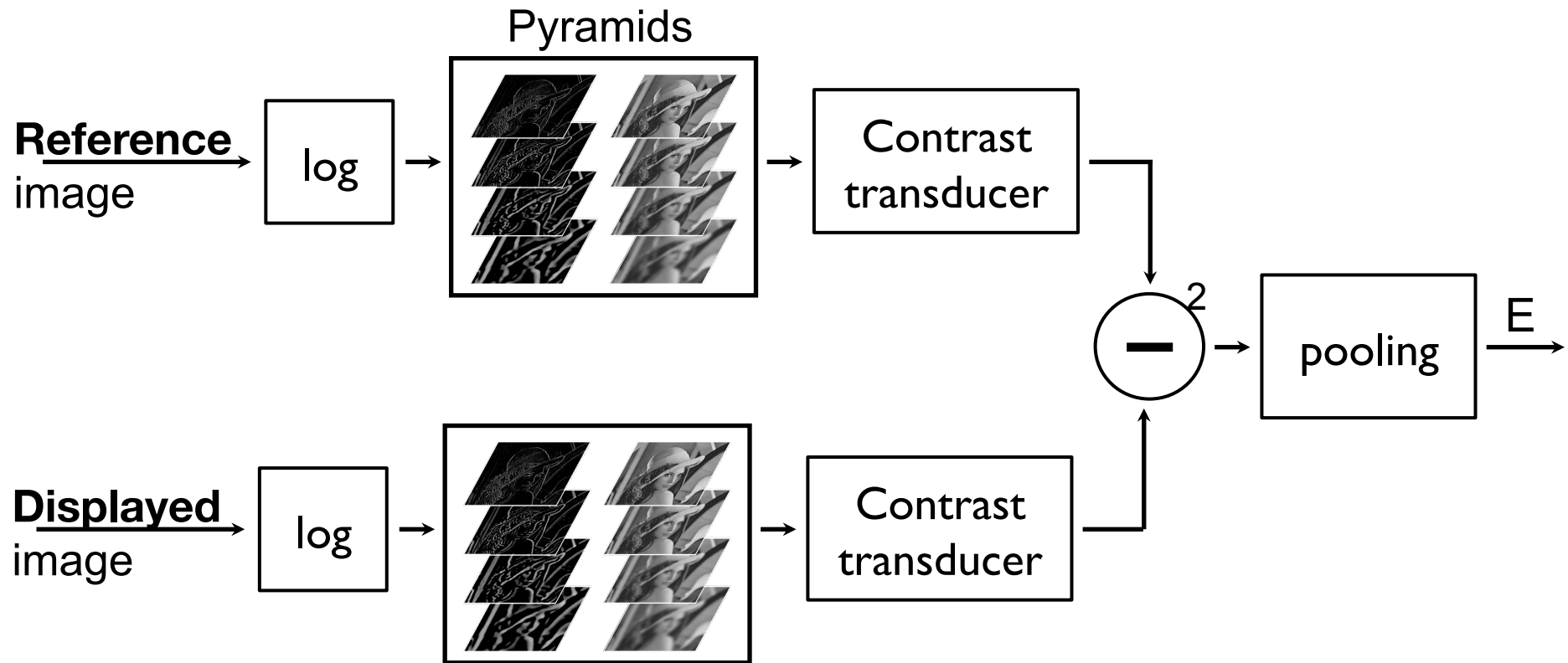
Visual metric

Display model

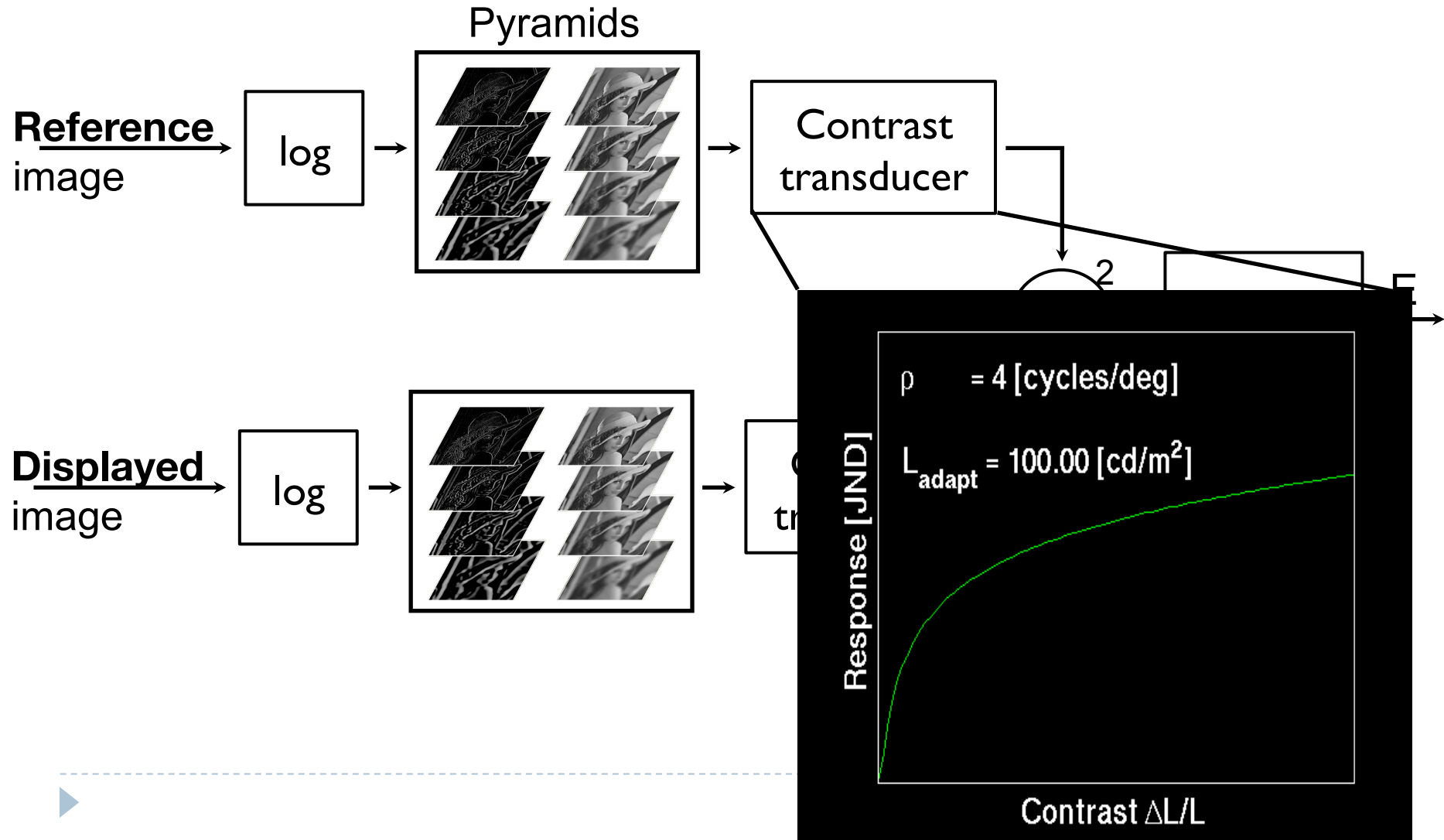
[Mantiuk et al., SIGGRAPH 2008]

# Visual metric

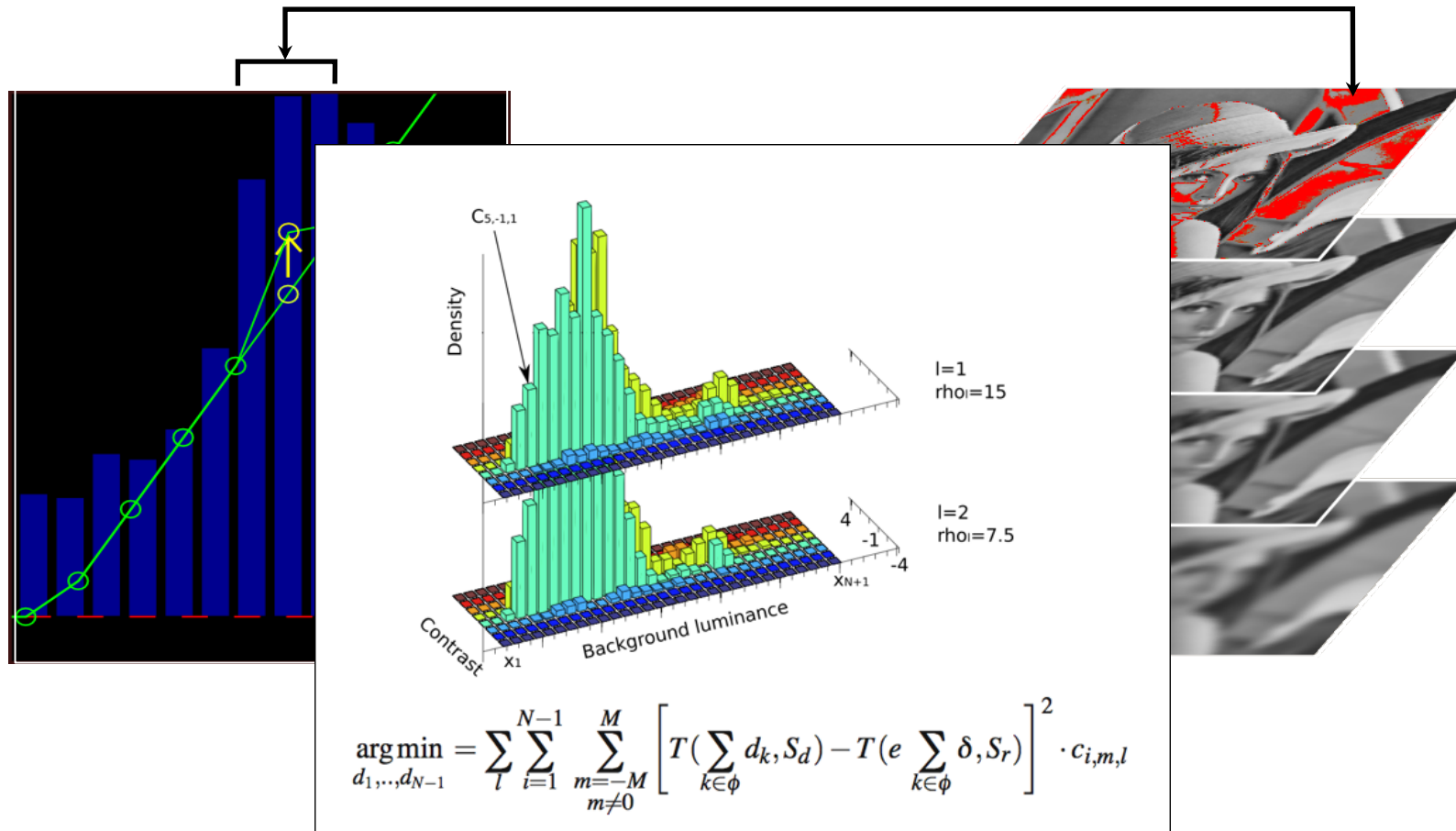
---



# Visual metric



# To accelerate: create a statistical model of an image



# Ambient illumination compensation

Non-adaptive TMO



Display adaptive TMO



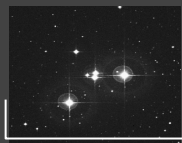
10<sup>80</sup>



# Ambient illumination compensation

Non-adaptive TMO

Display adaptive TMO



10



300



10 000

lux

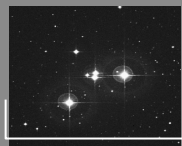


# Ambient illumination compensation

Non-adaptive TMO



Display adaptive TMO



$10^{82}$



300



10 000

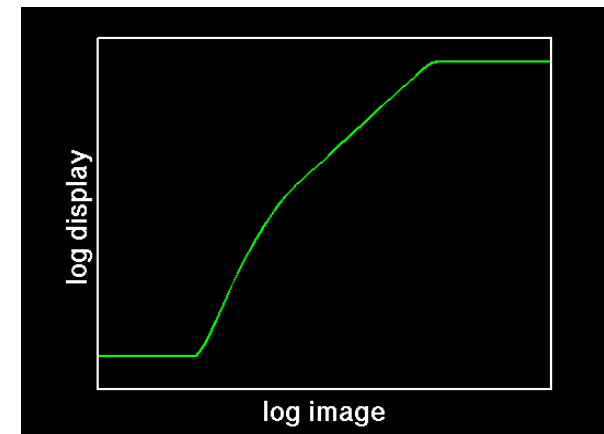
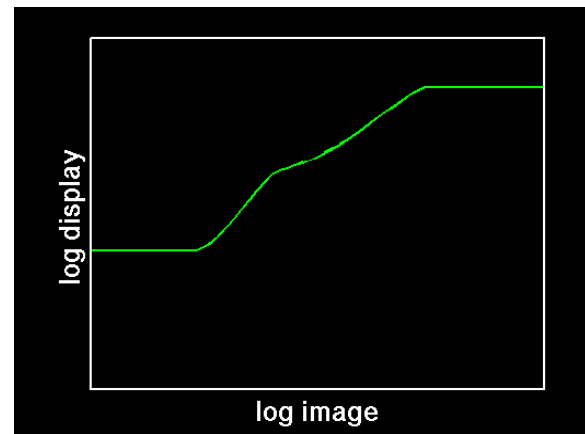
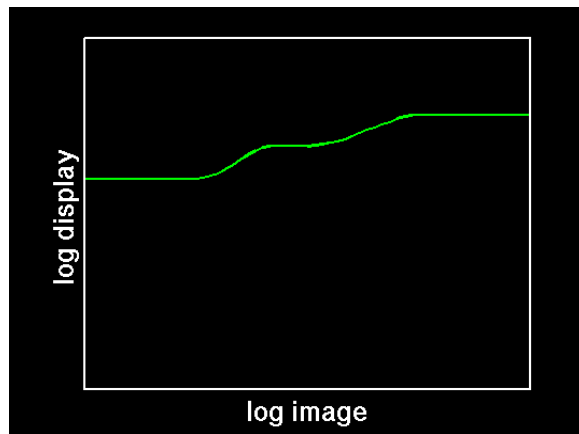
lux

# Results: display contrast

ePaper

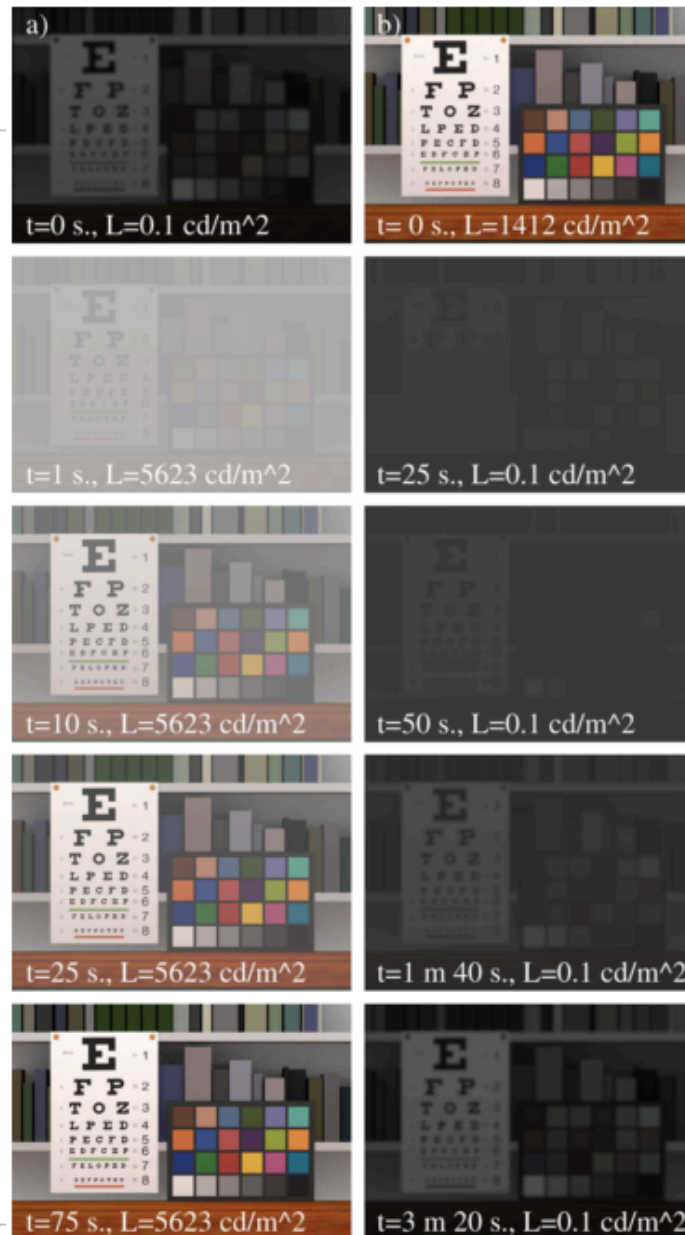
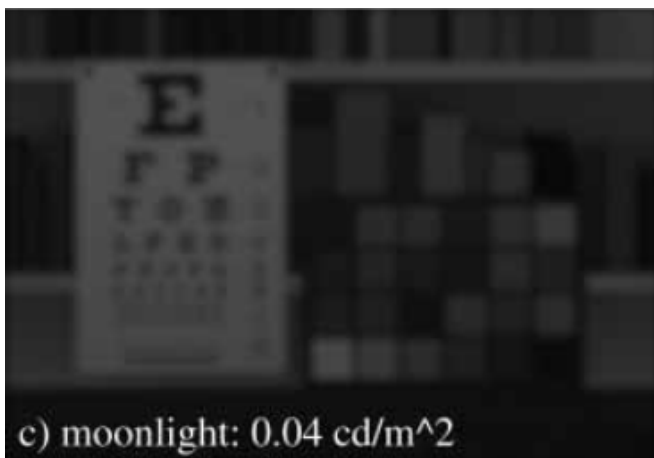
standard LCD

HDR display

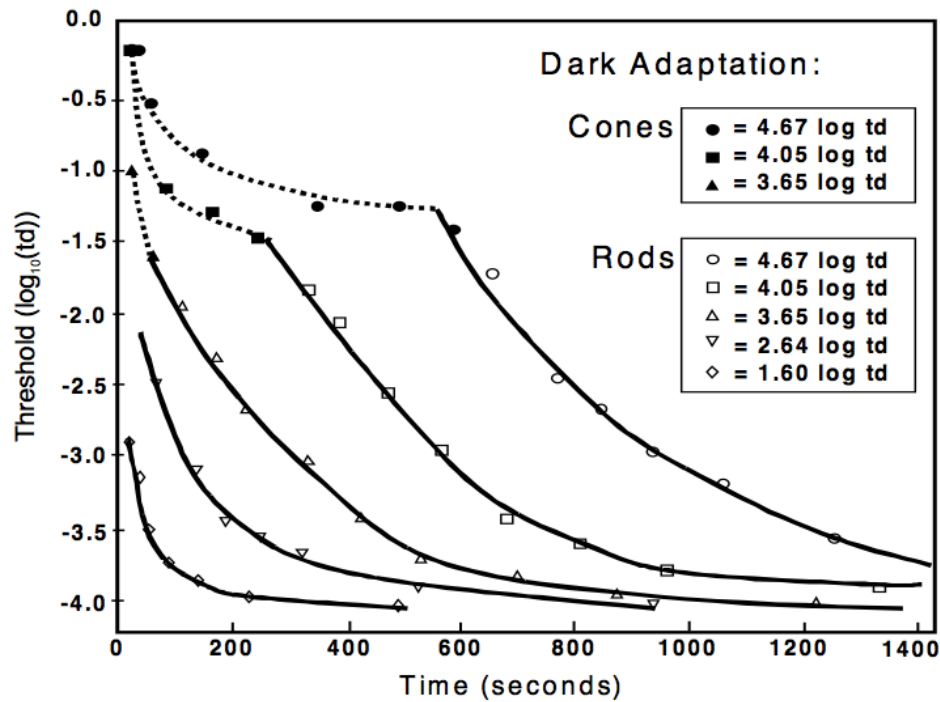


# Light and dark adaptation

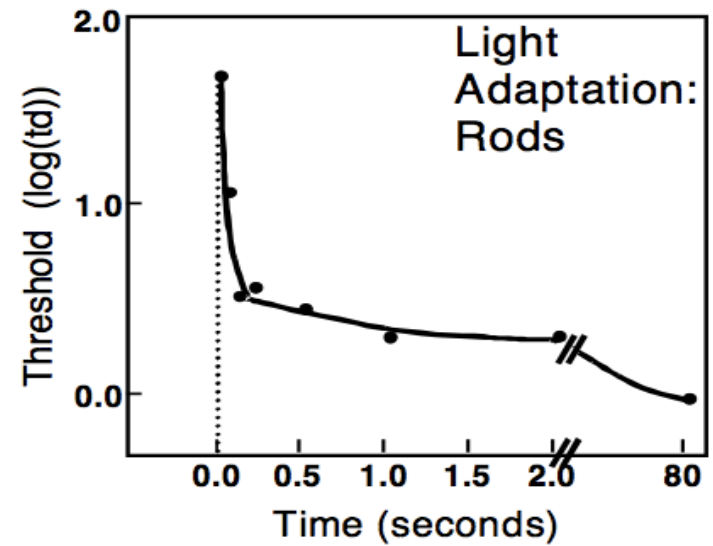
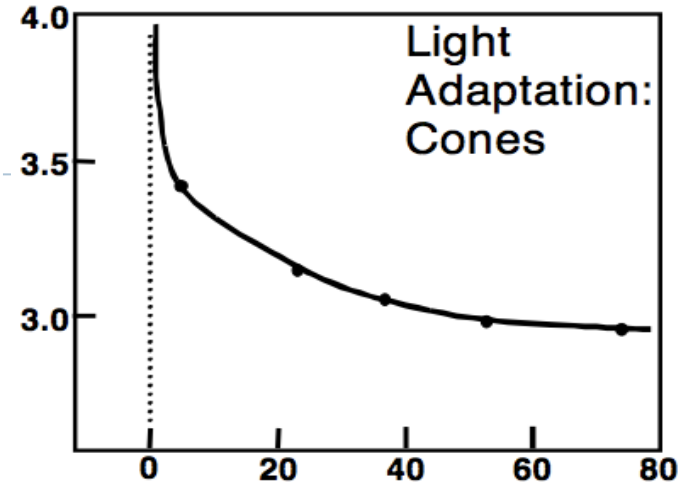
# Temporal adaptation



# Time-course of temporal adaptation



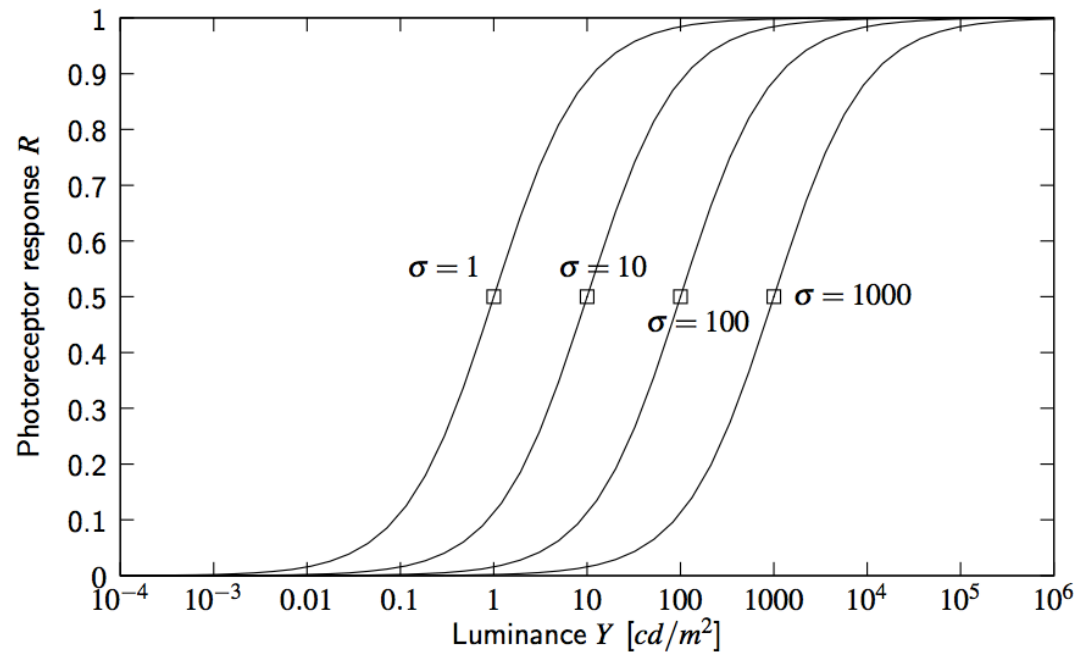
Bright -> Dark



Dark -> Bright

# In tone mapping: Photoreceptor models

## ► Naka-Rushton equation:



$$\frac{R}{R_{max}} = \frac{Y^n}{Y^n + \sigma^n}$$

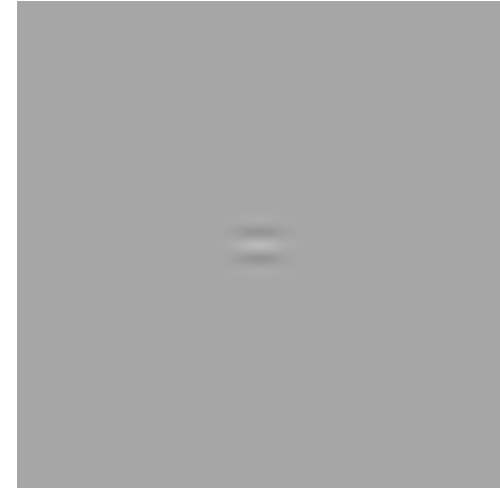
Depends on the  
luminance of  
adaptation



# How to find local adaptation?

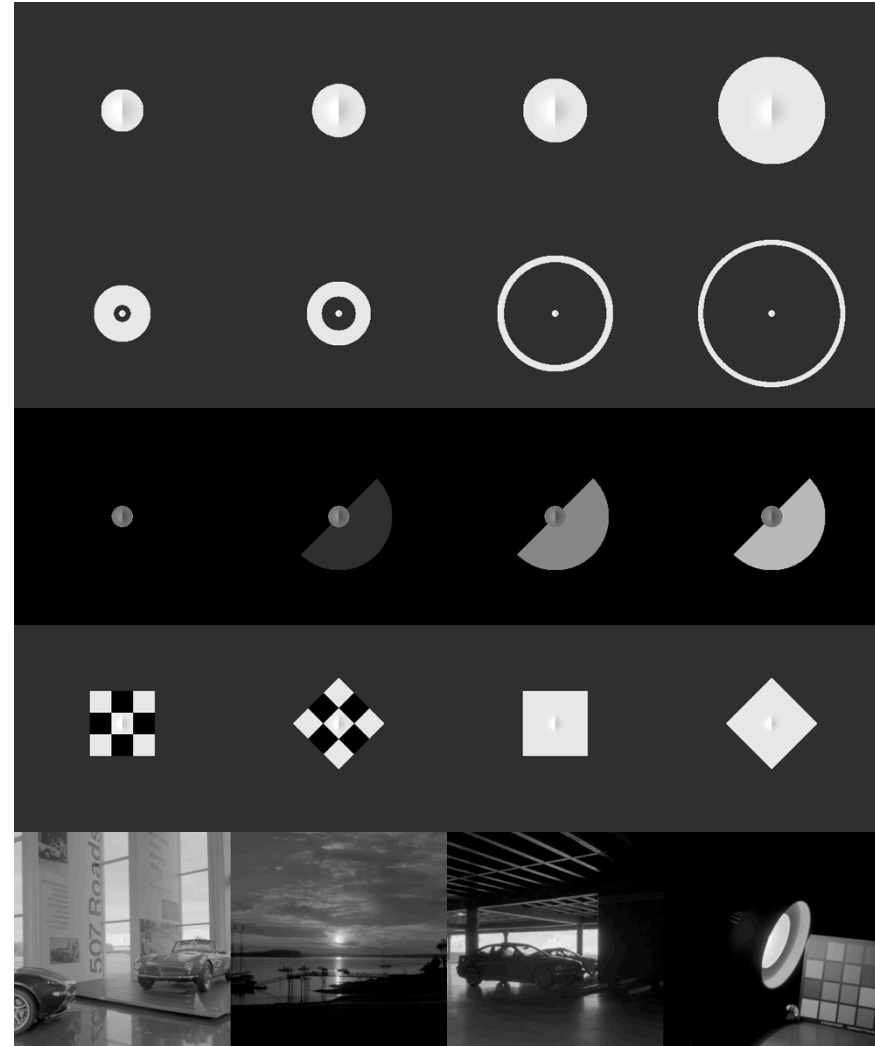
---

- ▶ In physiology and psychophysics
  - ▶ Uniform adapting field
    - ▶ Controlled conditions
  
- ▶ In computer graphics
  - ▶ Ad hoc assumptions
    - ▶ global average luminance
    - ▶ local per-pixel luminance
    - ▶ local average computed in  $1^\circ$  Gaussian window
    - ▶ ...



# Experiment: High contrast adaptation patterns on HDR display

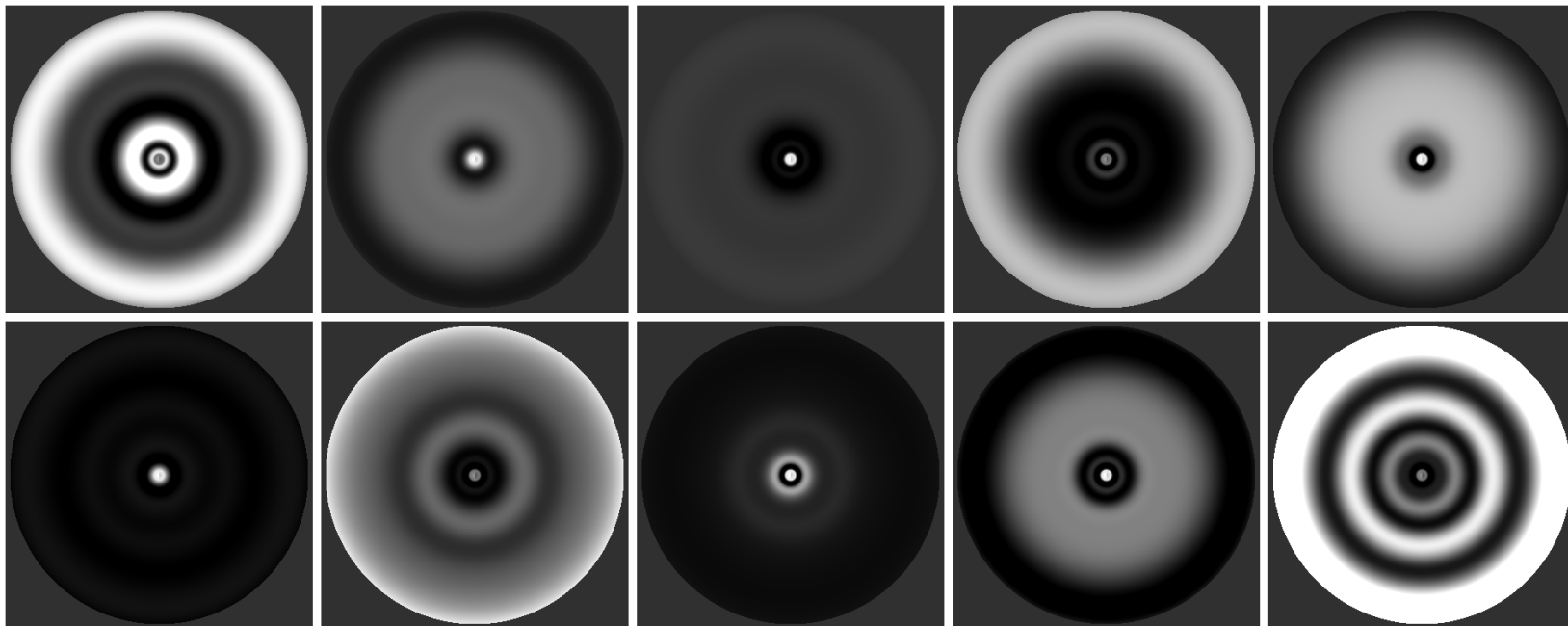
- ▶ Extent of pooling
- ▶ Long-range effects
- ▶ Pooling non-linearity
- ▶ Radial symmetry & contrast masking
- ▶ Natural images





# Optimized stimuli

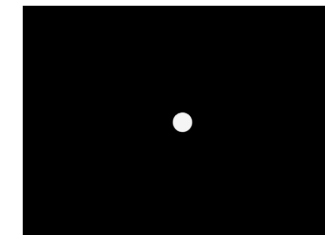
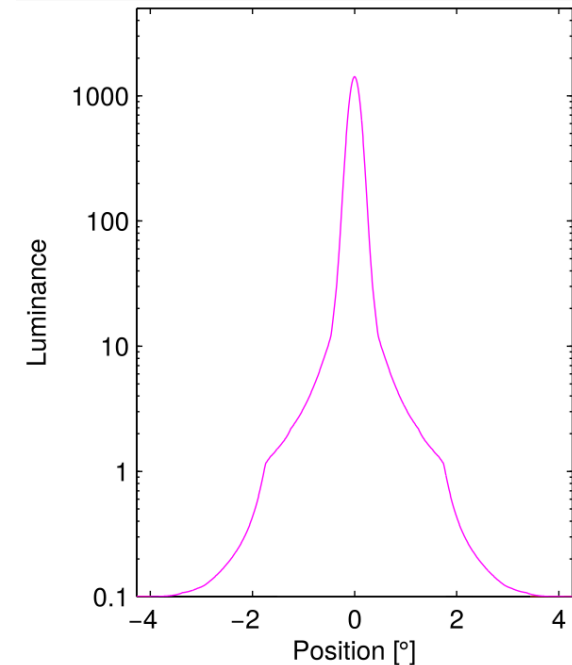
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# Local Adaptation Model

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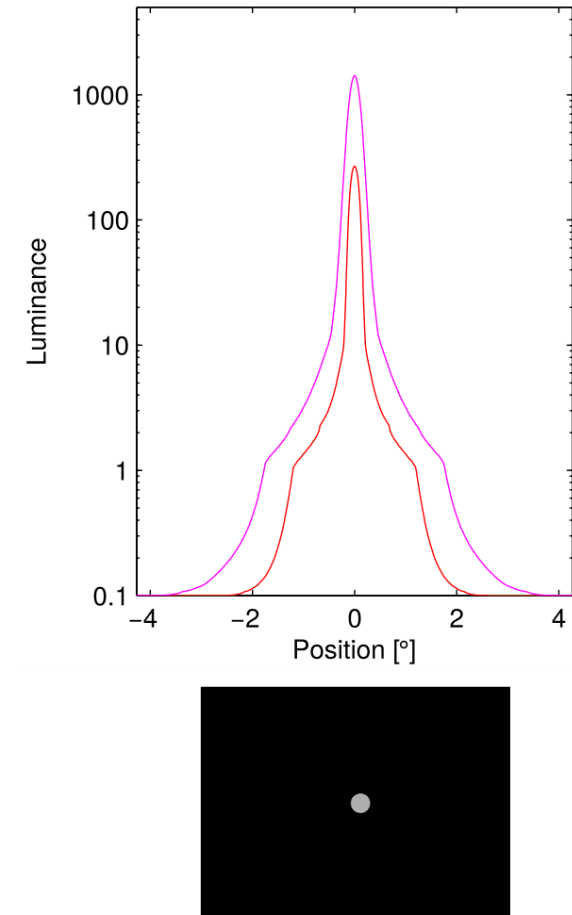
- ▶ **Wider support at lower luminance**
  - ▶ due to non-linearities
  - ▶ adaptation site shifts to postreceptoral mechanisms [Dunn et al. 2007]
- ▶ **Complex pooling mechanism**
  - ▶ cross-validated to avoid overfitting
  - ▶ more complex than known retinal pooling
  - ▶ receptive fields in LGN or visual cortex?



# Local Adaptation Model

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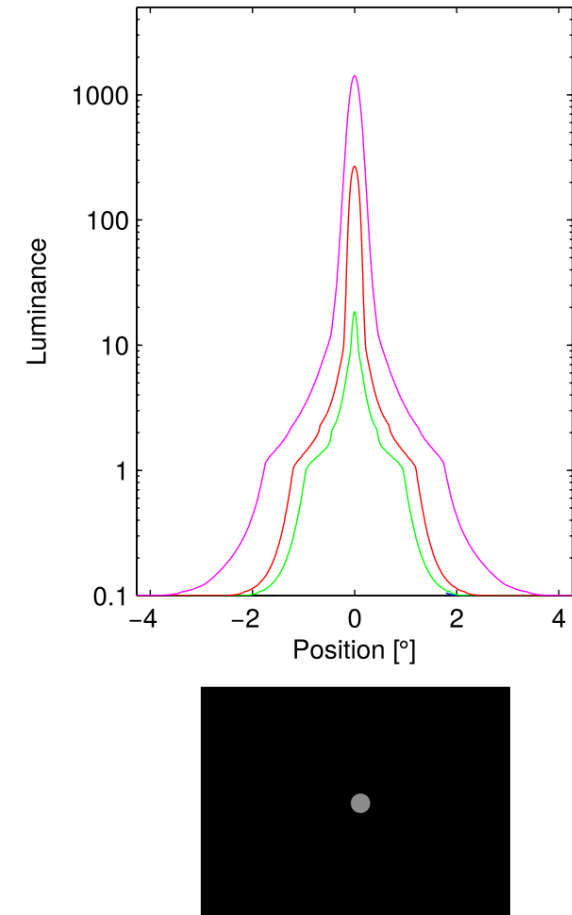
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- ▶ **Complex pooling mechanism**
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# Local Adaptation Model

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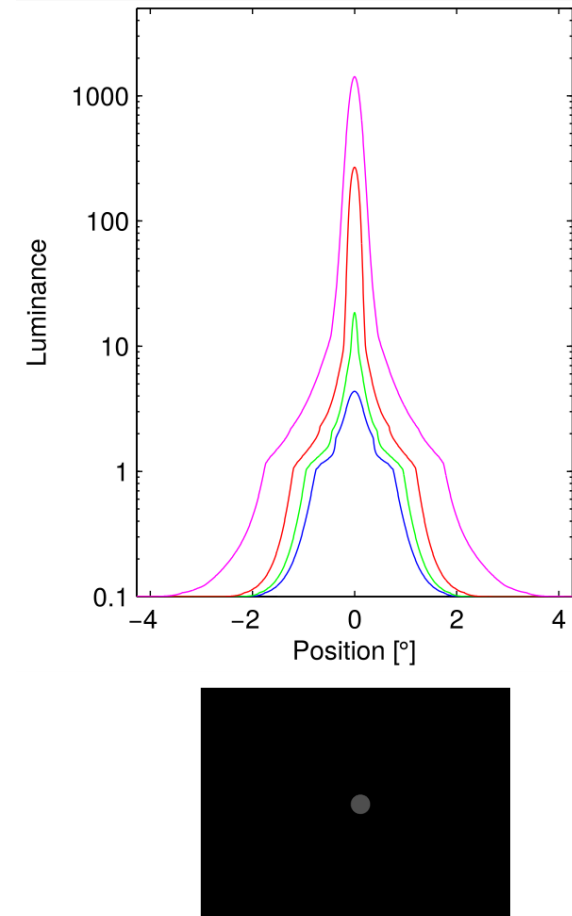
- ▶ **Wider support at lower luminance**
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# Local Adaptation Model

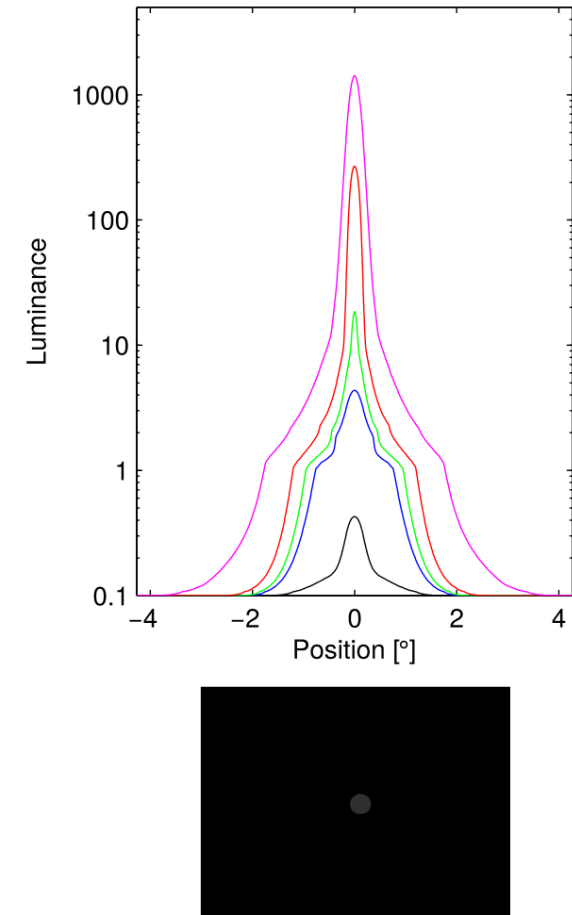
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- ▶ **Wider support at lower luminance**
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  - ▶ adaptation site shifts to postreceptoral mechanisms [Dunn et al. 2007]
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# Local Adaptation Model

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# Application: Gaze-dependent TM

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## **Applications**

**Gaze-dependent Tone Mapping**



# Summary

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- ▶ **Fundamentals**
  - ▶ Intents of tone-mapping
  - ▶ Display models
  - ▶ Four approaches to tone-mapping
- ▶ **Perceptual issues**
  - ▶ Color
  - ▶ Glare
  - ▶ Visual metrics-driven TMO
  - ▶ Light and dark adaptation

# References

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- ▶ Overview of HDR imaging & tone-mapping
  - ▶ [http://www.cl.cam.ac.uk/~rkm38/hdri\\_book.html](http://www.cl.cam.ac.uk/~rkm38/hdri_book.html)
- ▶ Papers on the simulation of glare
  - ▶ Spencer, G. et al. 1995. Physically-Based Glare Effects for Digital Images. Proceedings of SIGGRAPH. (1995), 325–334
  - ▶ Ritschel, T. et al. 2009. Temporal Glare: Real-Time Dynamic Simulation of the Scattering in the Human Eye. Computer Graphics Forum. 28, 2 (Apr. 2009), 183–192

Age-adaptive night vision

# Video 4

Rivoli

Simulation of age-adaptive night vision